Mango-Selm Software:
Fluid-Structure Interaction subject to Thermal Fluctuations
Soft Materials, Biophysics, Fluidics

August 2021, LAMMPS Workshop

Paul J. Atzberger

Department of Mathematics

Department of Mechanical Engineering

University of California Santa Barbara

DOE ASCR CM4
DE-SC0009254

DOE ASCR PhILMS
DE-SC0019246

NSF Grant
DMS - 1616353

NSF CAREER Grant
DMS-0956210

Tips for SELM Package: Installation and Usage

Instructions

Pre-compiled binaries: for (Debian 9+/Ubuntu and Centos 7+, Python 3.6+).

Quick start:
>> pip install selm-lammps
test: >> python -c "from selm_lammps.tests import t1; t1.test()“

Alternatively, can use *docker run -it ubuntu:20.04 /bin/bash; (use python3).*

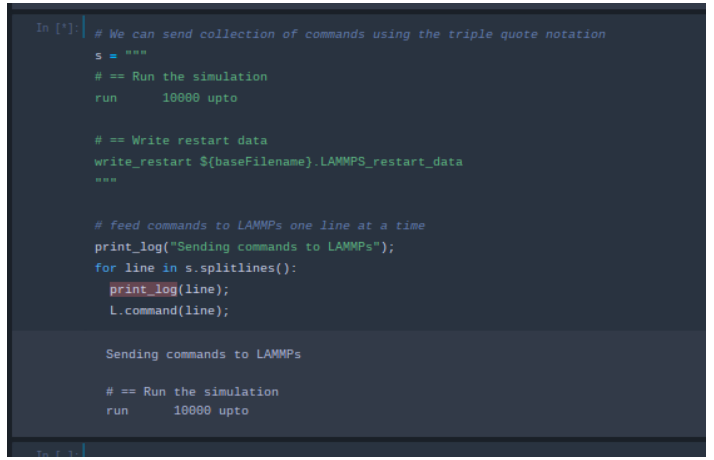
Examples, docs, source: see http://mango-selm.org/

Directories:
- src/USER-SELM: main C/C++ interface codes for SELM package
- examples/USER/selm: example models and simulation scripts
- lib/selm: library of SELM integrators and related algorithms

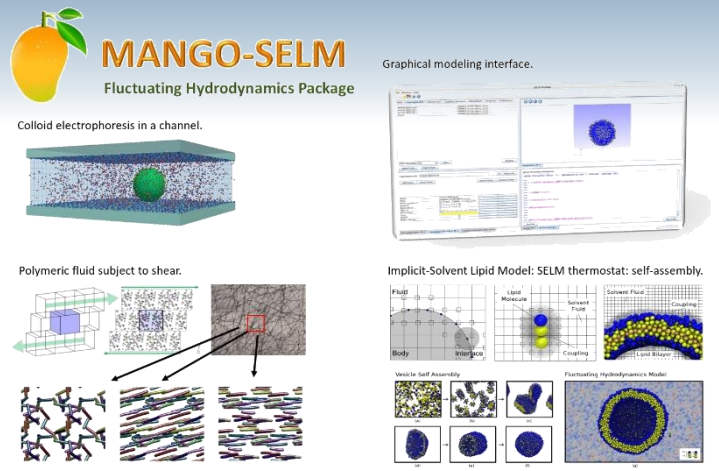
Installing Python components (uses lammps.py, lammps.so):
- Recommended to use *conda* or *virtualenv* with python >=3.6
- Examples for Jupyter notebooks, python scripts, for running simulations.
- See README files for more details.

Jupyter Notebooks and Python-based Simulations:
- Uses python-interfaces to LAMMPs.
- L.command(cmd_str); runs the command in cmd_str.
- Model building using python wrapper
  - sets up particles
  - sets up interactions, many possible types and potential available
  - sets up the simulation parameters.

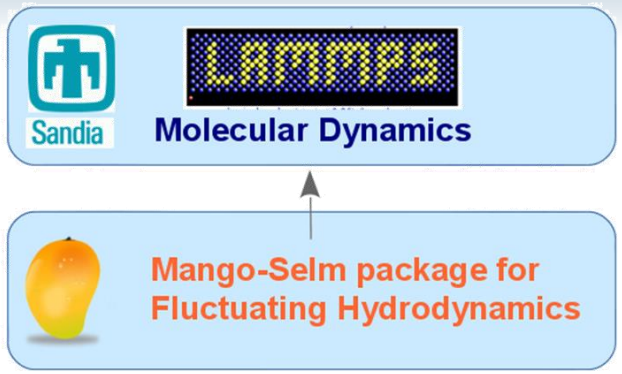
Python and Jupyter notebook interfaces



Mango-Selm Software: Overview



Molecular dynamics Integration



Python and Jupyter notebook interfaces

Download: http://mango-selm.org/

Selm - Simulation Package:

SELM fluctuating hydrodynamics for fluid-structure interactions subject to thermal fluctuations.

- **Python, Jupyter notebooks**, and other scripting for model building and simulation.
- **Stochastic numerical time-step integrators** for inertial and quasi-steady physical regimes in (C/C++).

Molecular dynamics integration with LAMMPS

- **Modeling, interactions, many potentials**, **statistical analysis**.
- **Thermostats and many ensembles possible** such as Lees-Edwards for shear simulations.

Standardized formats

- **XML** for parametrization and data output.
- **VTK** output for continuum fields and microstructures (visualization / analysis).

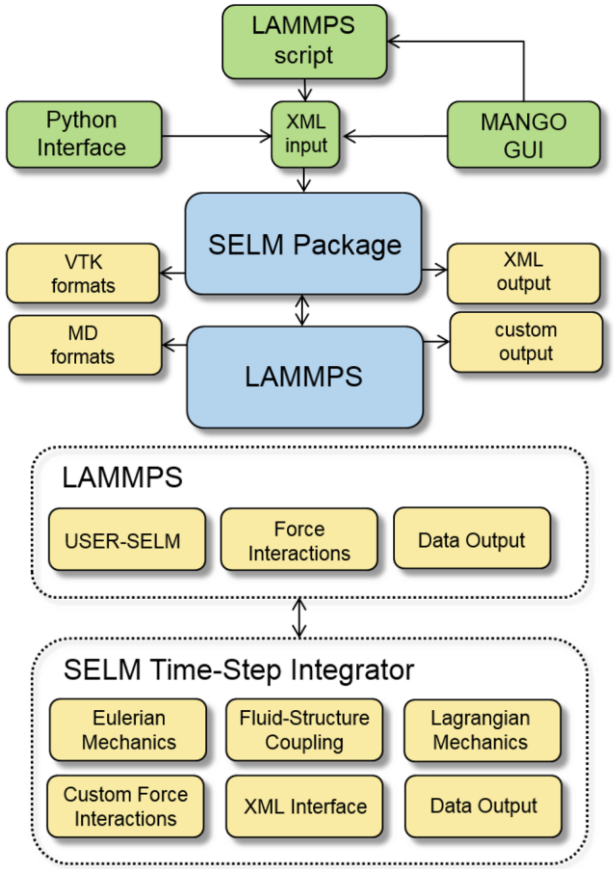
Mango – GUI for Model Building:

Graphical User Interface (GUI) for setting up model geometry and simulation parameters.

- **Generates scripts and data files** for SELM fluctuating hydrodynamics simulations.

Extendible object-oriented architectures for inclusion of new numerical methods.

Modular Design and Extendible

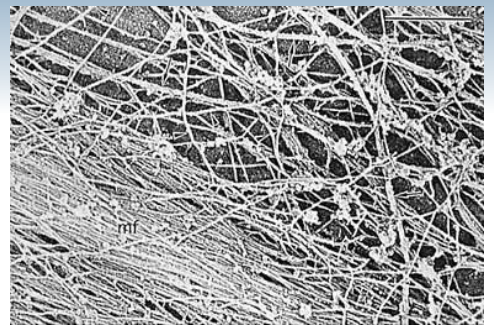


Atzberger 2016

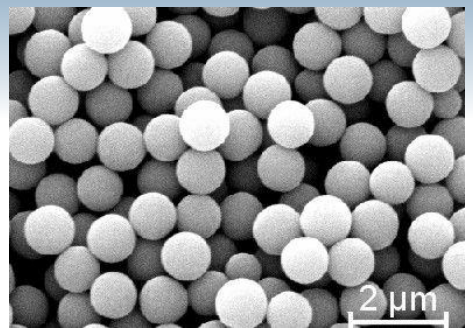
Motivations

Stochastic Immersed Boundary Methods (SIBMs)
Eulerian-Lagrangian Methods (ELMs)
Implicit-Solvent Coarse-Grained (IS-CG) Simulations

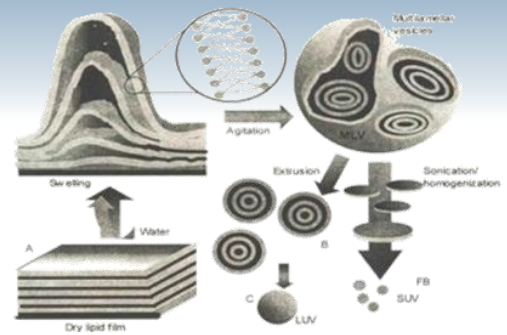
Motivations: Soft Materials, Complex Fluids, and Other Applications



Gels (Actin)



Colloids



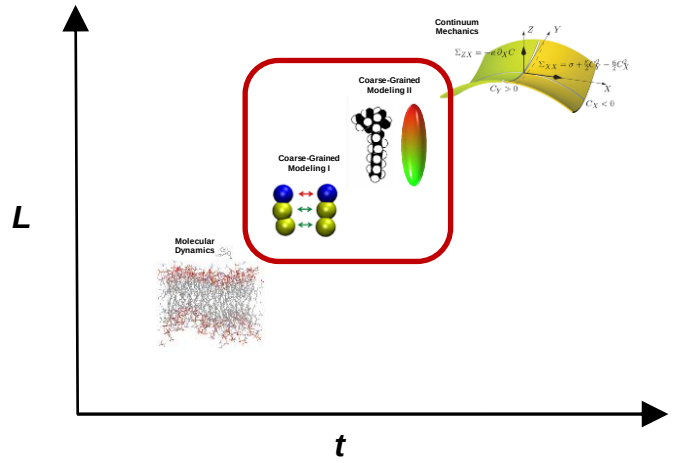
Membranes (lipids)

Soft Materials / Complex Fluids

- Microstructure interactions on the order of $K_B T$.
- Properties arise from balance of entropy-enthalpy.
- Solvent plays important role (interactions / dynamic responses).

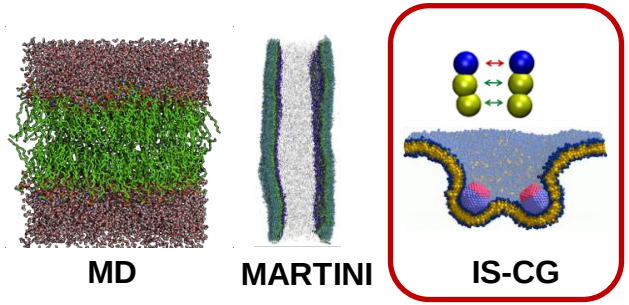
Approaches

- Atomistic Molecular Dynamics.
- Continuum Mechanics.
- Coarse-Grained Particle Models (solvated or implicitly treated).
- Challenges from phenomena spanning wide temporal-spatial scales.

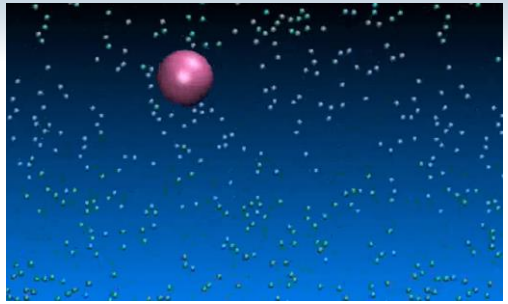


Simulation Aims

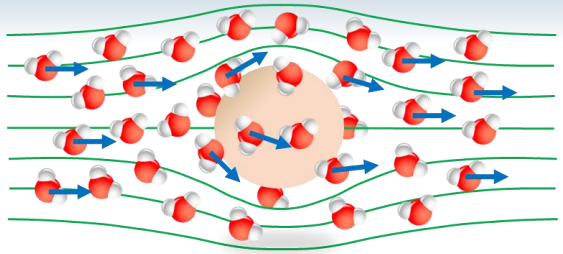
- Investigate how larger-scale mechanics arise from microstructure interactions / kinetics.
- Capture roles of solvent mediated interactions efficiently (i.e. continuum level).
- Resolve microstructure mechanics and dynamics.
- Computational efficiencies allow for accessing larger length and time-scales for investigating wider class of phenomena.



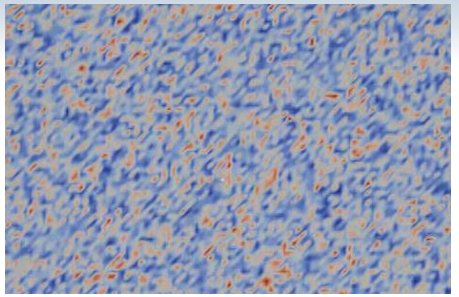
Fluctuating Hydrodynamics



Brownian Motion: Molecular Collisions



Hydrodynamics + Fluctuations



Continuum Gaussian Random Field

Landau-Lifschitz fluctuating hydrodynamics

$$\rho\left(\frac{\partial \mathbf{u}(\mathbf{x},t)}{\partial t}+\mathbf{u}(\mathbf{x},t)\cdot\nabla\mathbf{u}(\mathbf{x},t)\right)=\mu\Delta\mathbf{u}(\mathbf{x},t)-\nabla p(\mathbf{x},t)+\nabla\cdot\boldsymbol{\Sigma}(\mathbf{x},t).$$

$$\nabla\cdot\mathbf{u}(\mathbf{x},t)=0.$$

$$\langle\Sigma_{ij}(\mathbf{x},t)\Sigma_{kl}(\mathbf{y},s)\rangle=2\mu k_B T\left(\delta_{ik}\delta_{jl}+\delta_{il}\delta_{jk}\right)\delta(\mathbf{x}-\mathbf{y})\delta(t-s).$$

Fluctuations arise from spontaneous momentum transfer from molecular-level collisions.

Stochastic model of thermal fluctuations captured through random stress Σ ~ Gaussian.

Challenges for analysis and numerical methods presented from the δ-correlation in space-time.

Fluid-structure interactions: How to incorporate tractably?

Stochastic Eulerian Lagrangian Methods (SELMs) for Fluid-Structure Interactions

Fluid Equations

$$\begin{aligned} \rho\frac{\partial \mathbf{u}}{\partial t} &= \mathcal{L}\mathbf{u} + \Lambda[\Upsilon(\mathbf{v} - \Gamma\mathbf{u})] + \lambda + \mathbf{f}_{\text{thm}} \\ \nabla \cdot \mathbf{u} &= 0 \end{aligned}$$

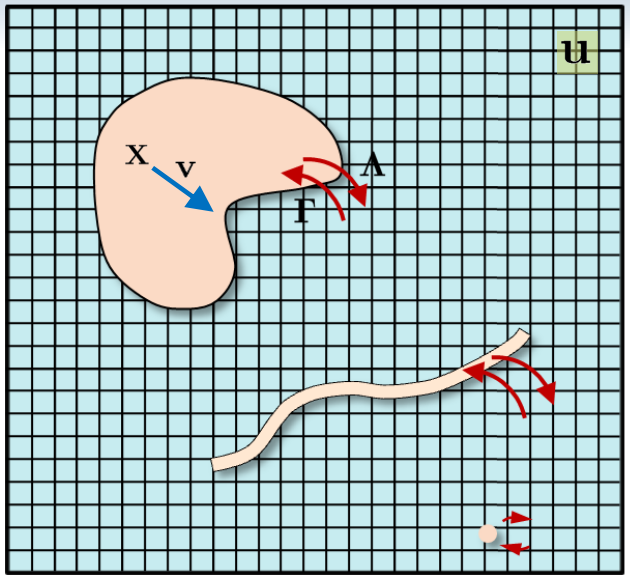
Microstructure Equations

$$\begin{aligned} \frac{d\mathbf{X}}{dt} &= \mathbf{v} \\ m\frac{d\mathbf{v}}{dt} &= -\Upsilon\left(\mathbf{v} - \Gamma\mathbf{u}\right) - \nabla_{\mathbf{X}}\Phi[\mathbf{X}] + \zeta + \mathbf{F}_{\text{thm}} \end{aligned}$$

Thermal Fluctuations

$$\begin{aligned} \langle \mathbf{f}_{\text{thm}}(s)\mathbf{f}^T_{\text{thm}}(t)\rangle &= -\left(2k_BT\right)\left(\mathcal{L} - \Lambda\Upsilon\Gamma\right)\delta(t-s) \\ \langle \mathbf{F}_{\text{thm}}(s)\mathbf{F}^T_{\text{thm}}(t)\rangle &= \left(2k_BT\right)\Upsilon\,\delta(t-s) \\ \langle \mathbf{f}_{\text{thm}}(s)\mathbf{F}^T_{\text{thm}}(t)\rangle &= -\left(2k_BT\right)\Lambda\Upsilon\,\delta(t-s). \end{aligned}$$

Eulerian-Lagrangian Approach



Operators:

- $\mathcal{L}$ ⟶ Fluid dissipation (viscosity).
- Υ ⟶ Structure "slip" relative to local flow field.
- Γ ⟶ Kinematic particle velocity for given flow.
- Λ ⟶ Induced fluid force density from particle.

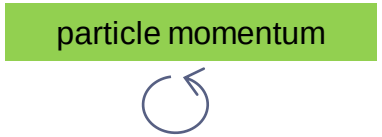
Notation:

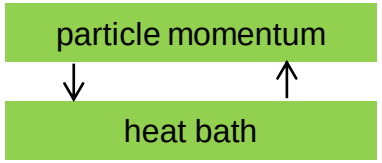
- $\mathbf{u} = \mathbf{u}(\mathbf{x}, t)$ ⟶ Fluid velocity.
- $\mathbf{X} = \mathbf{X}(\mathbf{q}, t)$ ⟶ Structure configuration
- $\mathbf{v} = \mathbf{v}(\mathbf{q}, t)$ ⟶ Structure velocity.

Peskin, Kramer, Atzberger 2007, Atzberger 2011

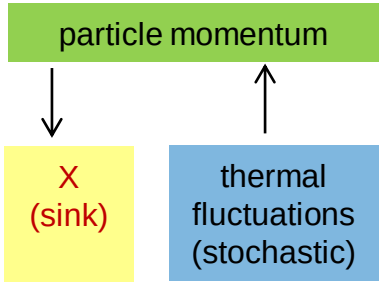
Thermostats

Berendson, Nose-Hoover





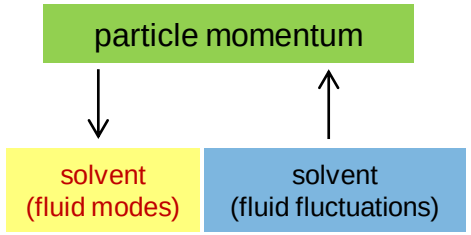
Langevin



$$
\begin{aligned}
m\frac{d\mathbf{V}}{dt} &= -\gamma\mathbf{V} - \nabla\Phi(\mathbf{X}) + \sqrt{2k_BT\gamma}\frac{d\mathbf{B}_t}{dt} \\
\frac{d\mathbf{X}}{dt} &= \mathbf{V}.
\end{aligned}
$$

missing correlations through solvent!

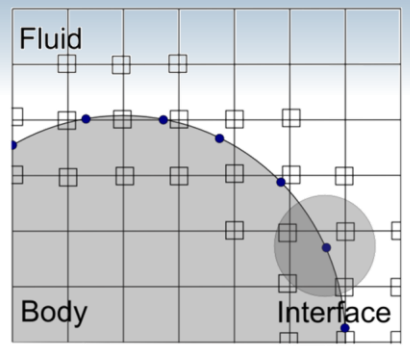
Fluctuating Hydrodynamics

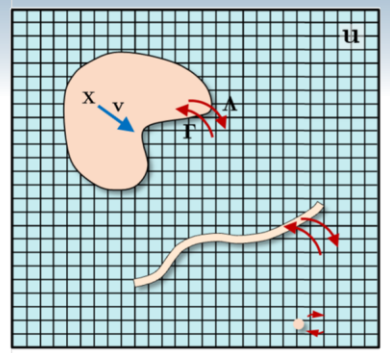


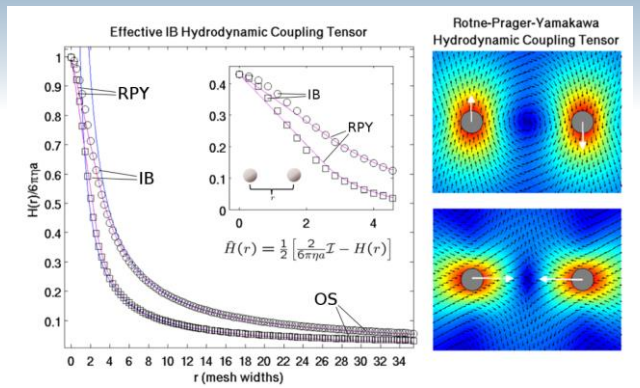
$$
\begin{aligned}
\frac{d\mathbf{X}}{dt} &= \mathbf{v} \\
m\frac{d\mathbf{v}}{dt} &= -\Upsilon\left(\mathbf{v} - \Gamma\mathbf{u}\right) - \nabla_{\mathbf{X}}\Phi[\mathbf{X}] + \zeta + \mathbf{F}_{\text{thm}}
\end{aligned}
$$

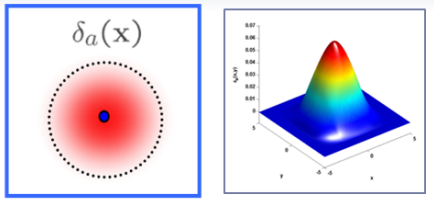
lateral momentum transfer : correlations

Coupling Operators, Immersed Boundary Methods









Peskin delta-function

SELM Coupling:

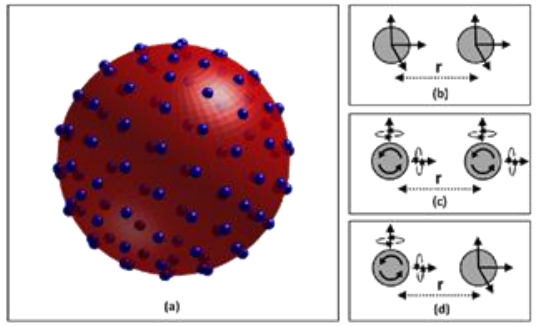
adjoint condition

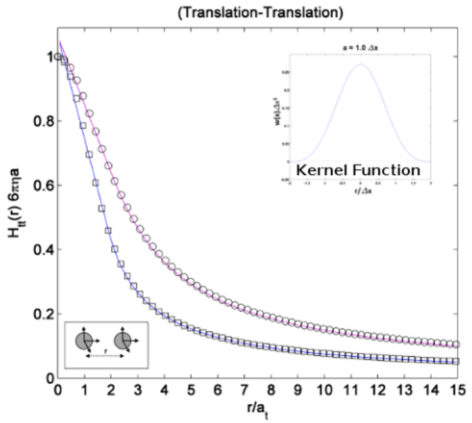
$$\langle \Gamma \mathbf{v}, \mathbf{F} \rangle \;=\; \sum_i [\Gamma \mathbf{v}]_i \cdot [\mathbf{F}]_i \;=\; \int_\Omega \mathbf{v}(\mathbf{x}) \cdot (\Lambda \mathbf{F})(\mathbf{x}) d\mathbf{x} \;=\; \langle \mathbf{v}, \Lambda \mathbf{F} \rangle$$

IB-Kernel coupling:

$$\Gamma \mathbf{u} \;=\; \int_\Omega \eta(\mathbf{y} - \mathbf{X}(t))\, \mathbf{u}(\mathbf{y}, t) d\mathbf{y}$$

$$\Lambda \mathbf{F} \;=\; \eta(\mathbf{x} - \mathbf{X}(t))\, \mathbf{F}.$$





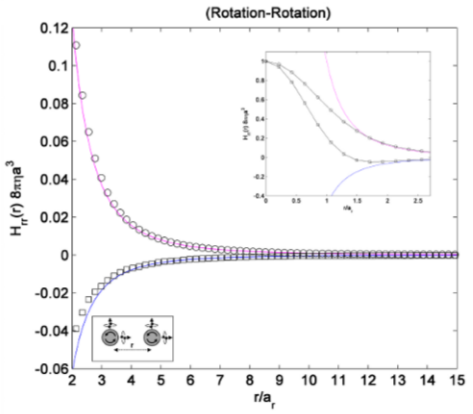
Generalized Coupling (Faxen)

$$\Gamma_0 \mathbf{u} = \sum_{\mathbf{m}} \left\langle\, \eta_0(\mathbf{y_m} - (\mathbf{X}_{\rm cm} + \mathbf{z}))\; \mathbf{u_m} \,\right\rangle_{\tilde{\mathcal{S}}, |\mathbf{z}|=R} \Delta x^3_{\mathbf{m}}$$

$$\Gamma_1 \mathbf{u} = \frac{3}{2R^2} \sum_{\mathbf{m}} \left\langle\, \eta_1(\mathbf{y_m} - (\mathbf{X}_{\rm cm} + \mathbf{z}))\, (\mathbf{z} \times \mathbf{u_m}) \,\right\rangle_{\tilde{\mathcal{S}}, |\mathbf{z}|=R} \Delta x^3_{\mathbf{m}}.$$

$$\Lambda_0(\mathbf{x_m}) = \left(\left\langle\, \eta_0(\mathbf{x_m} - (\mathbf{X}_{\rm cm} + \mathbf{z})) \,\right\rangle_{\tilde{\mathcal{S}}, |\mathbf{z}|=R} \right) \mathbf{F}$$

$$\Lambda_1(\mathbf{x_m}) = -\frac{3}{2R^2} \left(\left\langle\, \mathbf{z} \eta_1(\mathbf{x_m} - (\mathbf{X}_{\rm cm} + \mathbf{z})) \,\right\rangle_{\tilde{\mathcal{S}}, |\mathbf{z}|=R} \right) \times \mathbf{T}.$$



Summary of Regimes for SELMs

Stochastic Eulerian Lagrangian Methods (SELMs)

Fluid dynamics:

$$\begin{aligned}\rho\frac{\partial \mathbf{u}}{\partial t} &= \mu\Delta\mathbf{u} - \nabla p + \Lambda[\Upsilon(\mathbf{v}-\Gamma\mathbf{u})] + \mathbf{f}_{\text{thm}}\\ \nabla\cdot\mathbf{u} &= 0\end{aligned}$$

Structure dynamics:

$$\begin{aligned}\frac{d\mathbf{X}}{dt} &= \mathbf{v}\\ m\frac{d\mathbf{v}}{dt} &= -\Upsilon\left(\mathbf{v}-\Gamma\mathbf{u}\right) - \nabla_{\mathbf{X}}\Phi[\mathbf{X}] + \zeta + \mathbf{F}_{\text{thm}}\end{aligned}$$

Thermal Fluctuations

$$\begin{aligned}\langle \mathbf{f}_{\text{thm}}(s)\mathbf{f}^T_{\text{thm}}(t)\rangle &= -\left(2k_BT\right)\left(\mu\Delta - \Lambda\Upsilon\Gamma\right)\delta(t-s)\\ \langle \mathbf{F}_{\text{thm}}(s)\mathbf{F}^T_{\text{thm}}(t)\rangle &= \left(2k_BT\right)\Upsilon\,\delta(t-s)\\ \langle \mathbf{f}_{\text{thm}}(s)\mathbf{F}^T_{\text{thm}}(t)\rangle &= -\left(2k_BT\right)\Lambda\Upsilon\,\delta(t-s).\end{aligned}$$

Microstructure density matched with fluid

$m \ll \rho\ell^3$

Fluid-structure dynamics:

$$\begin{aligned}\frac{d\mathbf{p}}{dt} &= \rho^{-1}\mathcal{L}\mathbf{p} + \Lambda[-\nabla_{\mathbf{X}}\Phi(\mathbf{X})] + \left(\nabla_{\mathbf{X}}\cdot\Lambda\right)k_BT + \lambda + \mathbf{g}_{\text{thm}}\\ \frac{d\mathbf{X}}{dt} &= \rho^{-1}\Gamma\mathbf{p} + \Upsilon^{-1}[-\nabla_{\mathbf{X}}\Phi(\mathbf{X})] + \zeta + \mathbf{G}_{\text{thm}}.\\ \nabla_{\mathbf{X}}\cdot\Lambda &= \text{Tr}[\nabla_{\mathbf{X}}\Lambda]\end{aligned}$$

Phase space compressibility (p,X).

Thermal Fluctuations:

$$\begin{aligned}\langle \mathbf{g}_{\text{thm}}(s)\mathbf{g}^T_{\text{thm}}(t)\rangle &= -\left(2k_BT\right)\mathcal{L}\,\delta(t-s)\\ \langle \mathbf{G}_{\text{thm}}(s)\mathbf{G}^T_{\text{thm}}(t)\rangle &= \left(2k_BT\right)\Upsilon^{-1}\,\delta(t-s)\\ \langle \mathbf{g}_{\text{thm}}(s)\mathbf{G}^T_{\text{thm}}(t)\rangle &= 0.\end{aligned}$$

- Structure momentum no longer tracked.
- Removes a source of stiffness.
- Non-conjugate Hamiltonian formulation yields metric-factor in phase-space.

Microstructure-fluid no-slip coupling (S-Immersed-Boundary)

$\Upsilon \to \infty$

Fluid-Structure Equations:

$$\begin{aligned}\frac{d\mathbf{p}}{dt} &= \rho^{-1}\mathcal{L}\mathbf{p} + \Lambda[-\nabla_{\mathbf{X}}\Phi(\mathbf{X})] + \left(\nabla_{\mathbf{X}}\cdot\Lambda\right)k_BT + \lambda + \mathbf{g}_{\text{thm}}\\ \frac{d\mathbf{X}}{dt} &= \rho^{-1}\Gamma\mathbf{p}\end{aligned}$$

Thermal Fluctuations:

$$\langle \mathbf{g}_{\text{thm}}(s)\mathbf{g}^T_{\text{thm}}(t)\rangle = -\left(2k_BT\right)\mathcal{L}\,\delta(t-s).$$

- Structure dynamics no-longer inertial.
- Removes additional sources of stiffness.
- Regime of the Stochastic Immersed Boundary Method.
- Phase-space metric reflected in the drift term.

Microstructure-fluid stress balance

$\mu \to \infty$

Fluid-Structure Equations:

$$\begin{aligned}\frac{d\mathbf{X}}{dt} &= H_{\text{SELM}}[-\nabla_{\mathbf{X}}\Phi(\mathbf{X})] + \left(\nabla_{\mathbf{X}}\cdot H_{\text{SELM}}\right)k_BT + \mathbf{h}_{\text{thm}}\\ H_{\text{SELM}} &= \Gamma(-\wp\mathcal{L})^{-1}\Lambda\end{aligned}$$

Thermal Fluctuations:

$$\langle \mathbf{h}_{\text{thm}}(s)\mathbf{h}^T_{\text{thm}}(t)\rangle = \left(2k_BT\right)H_{\text{SELM}}\,\delta(t-s).$$

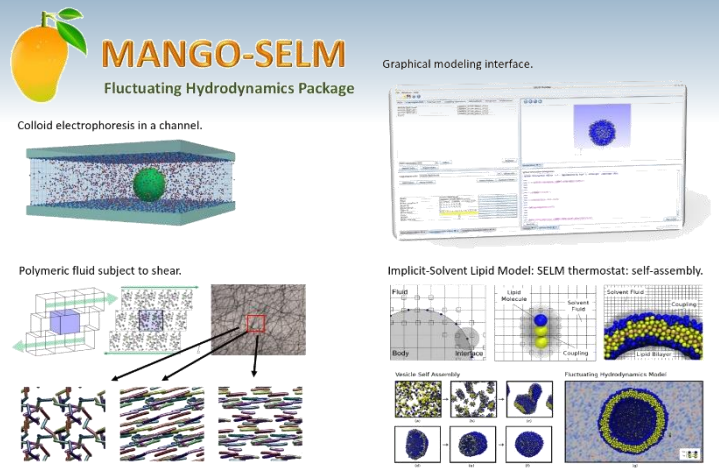
- Fluid momentum no longer tracked.
- Balance of hydrodynamic stresses with elastic stresses.
- Removes additional sources of stiffness.
- Regime of the Stokesian-Brownian Dynamics (Brady 1980, McCammond 1980's).
- Phase-space metric reflected in the drift term.

Atzberger & Tabak 2015

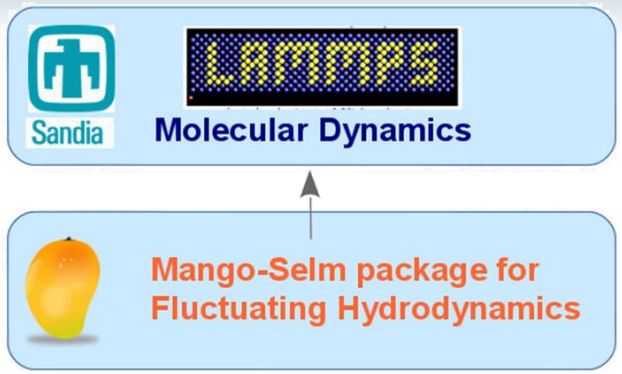
SELM-LAMMPS Integration

Molecular Dynamics and Coarse-Grained Modeling Approaches

Mango-Selm Software: Overview



Molecular dynamics Integration



Python and Jupyter notebook interfaces

Download: http://mango-selm.org/

Selm - Simulation Package:

SELM fluctuating hydrodynamics for fluid-structure interactions subject to thermal fluctuations.

- **Python, Jupyter notebooks**, and other scripting for model building and simulation.
- **Stochastic numerical time-step integrators** for inertial and quasi-steady physical regimes in (C/C++).

Molecular dynamics integration with LAMMPS

- **Modeling, interactions, many potentials**, **statistical analysis**.
- **Thermostats and many ensembles possible** such as Lees-Edwards for shear simulations.

Standardized formats

- **XML** for parametrization and data output.
- **VTK** output for continuum fields and microstructures (visualization / analysis).

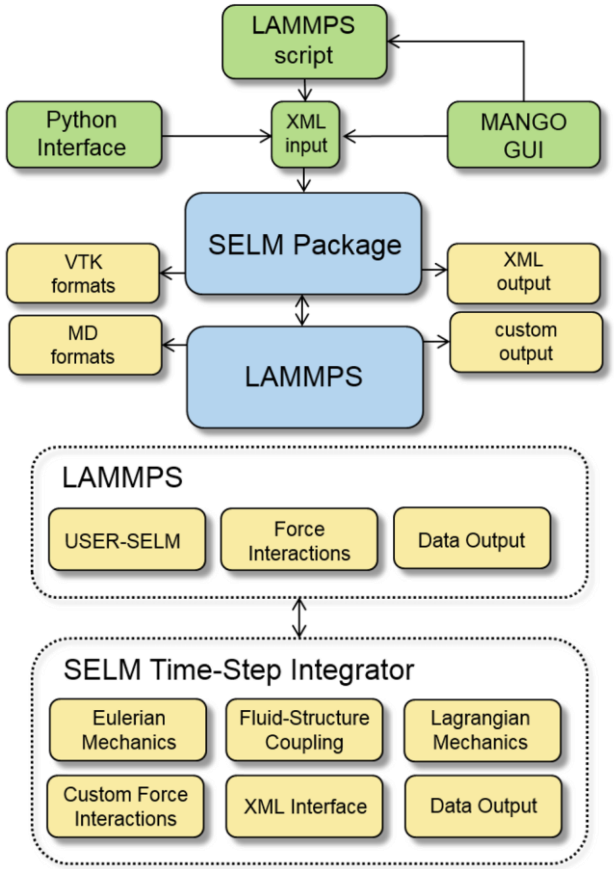
Mango – GUI for Model Building:

Graphical User Interface (GUI) for setting up model geometry and simulation parameters.

- **Generates scripts and data files** for SELM fluctuating hydrodynamics simulations.

Extendible object-oriented architectures for inclusion of new numerical methods.

Modular Design and Extendible



Atzberger 2016

Mango-Selm Implementation

Selm Codes: Design and Implementation

SELM – Source Codes:

LAMMPS-SELM Interface	XML Interface
fix_SELM.cpp	Atz_XML_Helper_ParseData.cpp
fix_SELM_XML_Handler.cpp	Atz_XML_Package.cpp
SELM_Package.cpp	Atz_XML_Parser.cpp
Atz_XML_Handler_Example_A.cpp	Atz_XML_SAX_DataHandler.cpp
Atz_XML_Helper_DataHandler_List.cpp	Atz_XML_SAX_Handler_Multilevel.cpp
Atz_XML_Helper_Handler_SkipNextTag.cpp	Atz_XML_SAX_Handler_PrintToScreen.cpp
Eulerian Mechanics	Lagrangian Mechanics
SELM_Eulerian.h	SELM_Lagrangian.h
SELM_Eulerian_Types.h	SELM_Lagrangian_Delegator_XML_Handler.h
SELM_Eulerian_Delegator_XML_Handler.h	SELM_Lagrangian_LAMMPS_ATOM_ANGLE_STYLE.h
SELM_Eulerian_LAMMPS_SHEAR_UNIFORM1_FFTW3.h	SELM_Lagrangian_LAMMPS_ATOM_ANGLE_STYLE_XML_Handler.h
SELM_Eulerian_LAMMPS_SHEAR_UNIFORM1_FFTW3_XML_Handler.h	SELM_Lagrangian_Types.h
SELM_Eulerian_Uniform1_Periodic.h	SELM_Package.h
SELM_Eulerian_Uniform1_Periodic_XML_Handler.h	
Time-Step Integration	Fluid-Structure Coupling
SELM_Integrator.h	SELM_CouplingOperator.h
SELM_Integrator_Delegator_XML_Handler.h	SELM_CouplingOperator_Delegator_XML_Handler.h
SELM_Integrator_FFTW3_Period.h	SELM_CouplingOperator_LAMMPS_SHEAR_UNIFORM1_FFTW3_TABLE1.h
SELM_Integrator_LAMMPS_SHEAR_QUASI_STEADY1_FFTW3.h	SELM_CouplingOperator_LAMMPS_SHEAR_UNIFORM1_FFTW3_TABLE1_XML_Handler.h
SELM_Integrator_LAMMPS_SHEAR_QUASI_STEADY1_FFTW3_XML_Handler.h	

Features:

Object-oriented C++ classes mirroring parts of SELM with **XML parameter files.**
Delegator design pattern is used to control the work-flow.
Four main SELM classes correspond to:

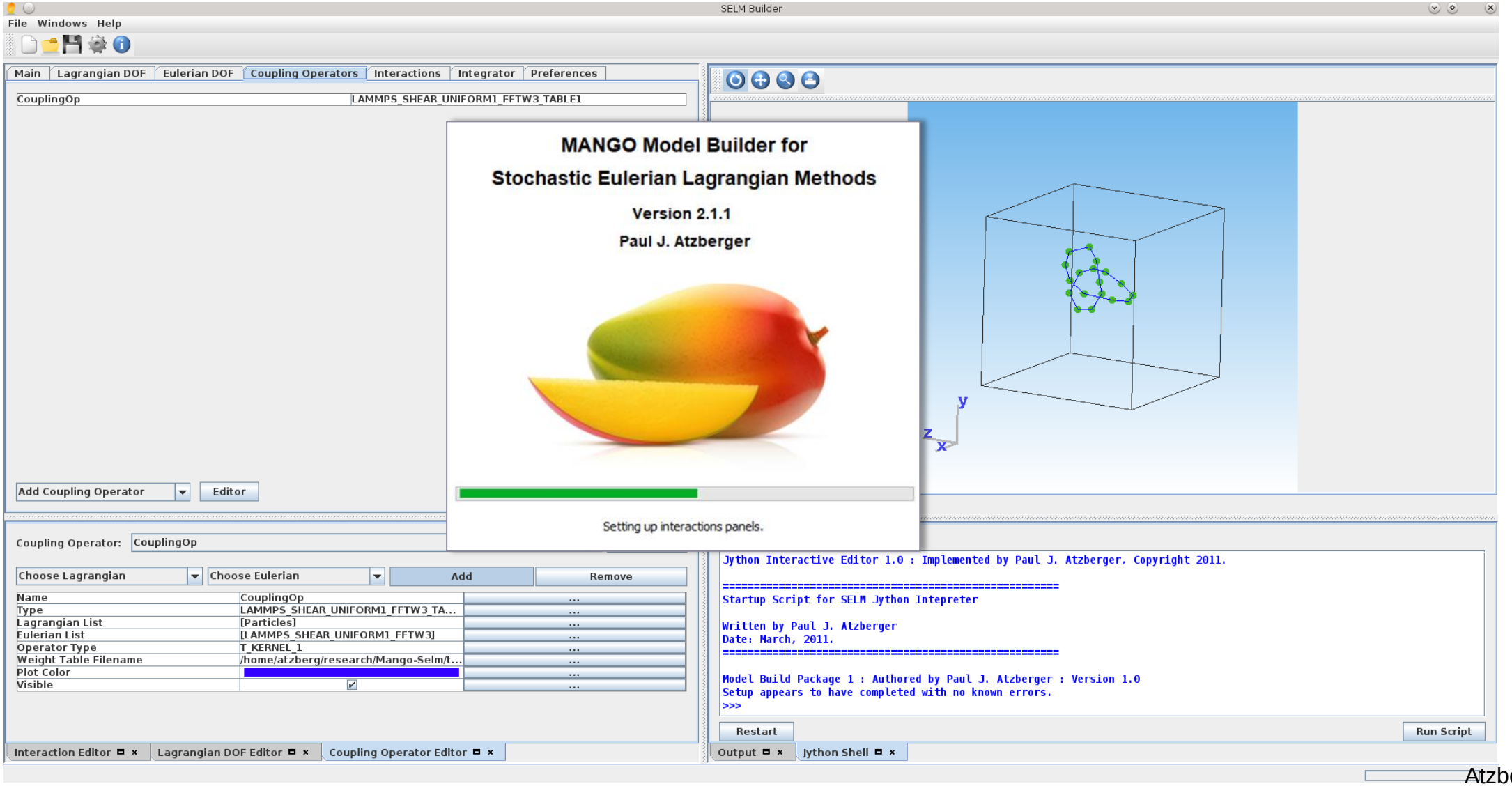
- Eulerian Mechanics
- Lagrangian Mechanics
- Fluid-Structure Coupling (Eulerian-Lagrangian communication)
- Time-Step Integration

Additional classes for XML parsing, data generation.
Designed to be easily extended for new types of SELM formulations and integrators.

Atzberger 2016

Mango GUI Model Builder

Mango - Modeling Software:



Atzberger 2016

Mango Modeling Software

Mango - Codes

SELM-Builder		
application_Main.java	JPanel_Lagrangian.java	SELM_RenderView.java
application_Project_Atz_XML_DataHandler_LAMMPS_USER_SELM.java	JPanel_Lagrangian_CONTROL_PTS_BASIC1.java	TableData_CouplingOperatorList.java
application_Project_Atz_XML_DataHandler_SELM_Builder.java	JPanel_Lagrangian_CONTROL_PTS_FAXEN1.java	TableData_EulerianList.java
application_SharedData.java	JPanel_Lagrangian_LAMMPS_ATOM_ANGLE_STYLE.java	TableData_EulerianList_old.java
application_Window_About.java	JPanel_Lagrangian_NULL.java	TableData_IntegratorList.java
application_Window_Main.java	JPanel_Lagrangian_SPECTRAL_FILAMENT1.java	TableData_InteractionList.java
application_Window_Main_SetupThread.java	JTable_CouplingOperator_LAMMPS_SHEAR_UNIFORM1_FFTW3_TABLE1.java	TableData_LagrangianList.java
application_Window_Splash.java	JTable_Interaction.java	TableData_LAMMPS_pair_coeff_tableFilename.java
Atz_Application_Data_Communication.java	JTable_Interaction_LAMMPS_ANGLES.java	TableEditor_CouplingOperatorList.java
Atz_ClassLoader.java	JTable_Interaction_LAMMPS_BONDS.java	TableEditor_EulerianList.java
Atz_ClassLoader_RegistryInfo.java	JTable_Interaction_LAMMPS_CUSTOM1.java	TableEditor_IntegratorList.java
Atz_DataChangeable.java	JTable_Interaction_LAMMPS_PAIR_COEFF.java	TableEditor_InteractionList.java
Atz_DataChangeEvent.java	JTable_Interaction_LAMMPS_PAIRS_HARMONIC.java	TableEditor_LagrangianList.java
Atz_DataChangeListener.java	JTable_Interaction_LAMMPS_SPECIAL_BONDS.java	TableEditor_LAMMPS_PAIR_COEFF_tableFilename.java
Atz_File_Generator.java	JTable_Interaction_PAIRS_HARMONIC.java	TableModel_CouplingOperator.java
Atz_File_Generator_LAMMPS_USER_SELM1.java	JTable_Lagrangian_ControlPts_BASIC1.java	TableModel_CouplingOperator_IB1.java
Atz_FileFilter.java	JTable_Langrangian_CONTROL_PTS.java	TableModel_CouplingOperator_LAMMPS_SHEAR_UNIFORM1_FFTW3_TABLE1.java
Atz_Helper_Generic.java	JTable_MainData.java	TableModel_CouplingOperator_TABLE1_tmp.java
Atz_Object_Factory.java	JTable_MainData_XML_LAMMPS_USER_SELM.java	TableModel_CouplingOperatorList.java
Atz_Object_Factory_Generic.java	JTable_MainData_XML_SELM_Builder.java	TableModel_Eulerian.java
Atz_Struct_DataChangeEvent.java	JTable_Preferences_Other.java	TableModel_Eulerian_LAMMPS_SHEAR_UNIFORM1_FFTW3.java
Atz_Struct_DataChangeListener.java	JTable_Preferences_Rendering.java	TableModel_Eulerian_SHEAR_UNIFORM1_FFTW3.java
Atz_Struct_DataChangeListener_MainData.java	JTable_Preferences_TableDisplay.java	TableModel_Eulerian_SHEAR_UNIFORM1_FFTW3_old.java
Atz_Struct_DataChangeListener_Test1.java	JTableHeaderRender_Default1.java	TableModel_Integrator.java
Atz_Struct_DataContainer.java	SELM_CouplingOperator.java	TableModel_Integrator_LAMMPS_SHEAR_QUASI_STEADY1_FFTW3.java
Atz_Struct_DataContainer_MainData.java	SELM_CouplingOperator_IB1.java	TableModel_Integrator_LAMMPS_SHEAR1.java
Atz_Struct_DataListManager.java	SELM_CouplingOperator_LAMMPS_SHEAR_UNIFORM1_FFTW3_TABLE1.java	TableModel_Integrator_SELM_SHEAR1_old.java
Atz_XML_Helper_Handler_EulerianRef.java	SELM_CouplingOperator_NULL.java	TableModel_Integrator_SHEAR1.java
Atz_XML_Helper_Handler_LagrangianRef.java	SELM_CouplingOperator_XML_DataDelegator.java	TableModel_Interaction.java
JDialog_Edit_CouplingOperatorList.java	SELM_Eulerian.java	TableModel_Interaction_LAMMPS_ANGLES.java
JDialog_Edit_EulerianList.java	SELM_Eulerian_LAMMPS_SHEAR_UNIFORM1_FFTW3.java	TableModel_Interaction_LAMMPS_BONDS.java
JDialog_Edit_InteractionList.java	SELM_Eulerian_NULL.java	TableModel_Interaction_LAMMPS_CUSTOM1.java
JDialog_Edit_LagrangianList.java	SELM_Eulerian_SHEAR_UNIFORM1_FFTW3.java	TableModel_Interaction_LAMMPS_PAIR_COEFF.java
JDialog_FontSelector.java	SELM_Eulerian_UNIFORM1_FFTW3.java	TableModel_Interaction_LAMMPS_PAIRS_HARMONIC.java
JDialog_Generate_Simulation_Data_LAMMPS.java	SELM_Eulerian_XML_DataDelegator.java	TableModel_Interaction_LAMMPS_SPECIAL_BONDS.java
JDialog_Message_Generate_LAMMPS_USER_SELM.java	SELM_EulerianInterface_LAMMPS.java	TableModel_InteractionList.java
JFrame_SplashProgress.java	SELM_EulerianRenderView.java	TableModel_Lagrangian.java
JPanel_CouplingOperator.java	SELM_Integrator.java	TableModel_Lagrangian_CONTROL_PTS_BASIC1.java
JPanel_CouplingOperator_IB1.java	SELM_Integrator_BD1.java	TableModel_Lagrangian_CONTROL_PTS_FAXEN1.java
JPanel_CouplingOperator_LAMMPS_SHEAR_UNIFORM1_FFTW3_TABLE1.java	SELM_Integrator_LAMMPS_SHEAR_QUASI_STEADY1_FFTW3.java	TableModel_Lagrangian_LAMMPS_ATOM_ANGLE_STYLE.java
JPanel_CouplingOperator_NULL.java	SELM_Integrator_LAMMPS_SHEAR1.java	TableModel_Lagrangian_SPECTRAL_FILAMENT1.java
JPanel_Demo1.java	SELM_Integrator_NULL.java	TableModel_LagrangianList.java
JPanel_Edit_CouplingOpList.java	SELM_Integrator_SHEAR1.java	TableModel_MainData.java
JPanel_Edit_InteractionList.java	SELM_Integrator_XML_DataDelegator.java	TableModel_Preferences_Other.java
JPanel_Edit_LagrangianList.java	SELM_IntegratorInterface_LAMMPS.java	TableModel_Preferences_Rendering.java
JPanel_Editor_CouplingOperator.java	SELM_IntegratorRenderView.java	TableModel_Preferences_TableDisplay.java
JPanel_Editor_Eulerian_DOF.java	SELM_Interaction.java	TableModel_Properties1_Test1.java
JPanel_Editor_Integrator.java	SELM_Interaction_LAMMPS_ANGLES.java	TableRenderer_CouplingOperatorList.java
JPanel_Editor_Interaction.java	SELM_Interaction_LAMMPS_BONDS.java	TableRenderer_EulerianList.java
JPanel_Editor_Lagrangian_DOF.java	SELM_Interaction_LAMMPS_CUSTOM1.java	TableRenderer_IntegratorList.java
JPanel_Editor_Test1.java	SELM_Interaction_LAMMPS_PAIR_COEFF.java	TableRenderer_InteractionList.java
JPanel_Eulerian.java	SELM_Interaction_LAMMPS_PAIRS_HARMONIC.java	TableRenderer_LagrangianList.java
JPanel_Eulerian_interface_controlActionListener.java	SELM_Interaction_LAMMPS_SPECIAL_BONDS.java	TableRenderer_LAMMPS_pair_coeff_tableFilename.java
JPanel_Eulerian_LAMMPS_SHEAR_UNIFORM1_FFTW3.java	SELM_Interaction_NULL.java	XMLContentHandler.java
JPanel_Eulerian_NULL.java	SELM_Interaction_PAIRS_HARMONIC.java	3D Rendering
JPanel_Eulerian_SHEAR_UNIFORM1_FFTW3.java	SELM_Interaction_PAIRS_TABLE.java	Atz_LinearAlgebra.java
JPanel_Eulerian_UNIFORM1_FFTW3.java	SELM_Interaction_TARGET1.java	Atz3D_Camera.java
JPanel_Helper_CouplingOperator_GenericTable.java	SELM_Interaction_XML_DataDelegator.java	Atz3D_Element.java
JPanel_Helper_Eulerian_GenericTable.java	SELM_InteractionInterface_LAMMPS.java	Atz3D_Element_LinePairs.java
JPanel_Helper_Integrator_GenericTable.java	SELM_InteractionInterface_LAMMPS_ANGLES.java	Atz3D_Element_Lines.java
JPanel_Helper_Interaction_GenericTable.java	SELM_InteractionInterface_LAMMPS_BONDS.java	Atz3D_Element_Points.java
JPanel_Helper_Lagrangian_GenericTable.java	SELM_InteractionInterface_LAMMPS_PAIR_STYLE.java	Atz3D_Element_Points_DataClosest.java
JPanel_Integrator.java	SELM_InteractionInterface_LAMMPS_PAIR_STYLE_TABLE.java	Atz3D_Model.java
JPanel_Integrator_BD1.java	SELM_InteractionRenderView.java	Atz3D_Model_SELM.java
JPanel_Integrator_LAMMPS_SHEAR_QUASI_STEADY1_FFTW3.java	SELM_Lagrangian.java	Atz3D_Renderer.java
JPanel_Integrator_NULL.java	SELM_Lagrangian_CONTROL_PTS_BASIC1.java	Atz3D_Renderer_SELM.java
JPanel_Interaction.java	SELM_Lagrangian_CONTROL_PTS_FAXEN1.java	JPanel_Model_View_Composite.java
JPanel_Interaction_LAMMPS_ANGLES.java	SELM_Lagrangian_interface.java	JPanel_Model_View_Composite_XML_SELM_Builder.java
JPanel_Interaction_LAMMPS_BONDS.java	SELM_Lagrangian_LAMMPS_ATOM_ANGLE_STYLE.java	JPanel_Model_View_RenderPanel.java
JPanel_Interaction_LAMMPS_CUSTOM1.java	SELM_Lagrangian_NULL.java	JPanel_Model_View_RenderPanel_XML_SELM_Builder.java
JPanel_Interaction_LAMMPS_PAIR_COEFF.java	SELM_Lagrangian_SPECTRAL_FILAMENT1.java	Physical Units
JPanel_Interaction_LAMMPS_PAIRS_HARMONIC.java	SELM_Lagrangian_wrapper.java	Atz_Unit.java
JPanel_Interaction_LAMMPS_SPECIAL_BONDS.java	SELM_Lagrangian_XML_DataDelegator.java	Atz_UnitsData.java
JPanel_Interaction_NULL.java	SELM_LagrangianInterface_LAMMPS.java	Atz_UnitsRef.java
JPanel_Interaction_PAIRS_HARMONIC.java	SELM_LagrangianRef_XML_DataHandler.java	Atz_UnitsRef_PhysicalUnits.java
JPanel_Interaction_TARGET1.java	SELM_LagrangianRenderView.java	JDialog_Edit_Units_Ref.java

Atzberger 2016

Mango Modeling Software

MANGO - Codes

SELM-Builder	
application_Main.java	JPanel_Lagrangian.java
application_Project_Atz_XML_DataHandler_LAMMPS_USER_SELM.java	JPanel_Lagrangian_CONTROL_PTS_BASIC1.java
application_Project_Atz_XML_DataHandler_SELM_Builder.java	JPanel_Lagrangian_CONTROL_PTS_FAXEN1.java
application_SharedData.java	JPanel_Lagrangian_LAMMPS_ATOM_ANGLE_STYLE.java
application_Window_About.java	JPanel_Lagrangian_NULL.java
application_Window_Main.java	JPanel_Lagrangian_SPECTRAL_FILAMENT1.java
application_Window_Main_SetupThread.java	JTable_CouplingOperator_LAMMPS_SHEAR_UNIFORM1_FFTW3_TABLE1.java
application_Window_Splash.java	JTable_Interaction.java
Atz_Application_Data_Communication.java	JTable_Interaction_LAMMPS_ANGLES.java
Atz_ClassLoader.java	JTable_Interaction_LAMMPS_BONDS.java
Atz_ClassLoader_RegistryInfo.java	JTable_Interaction_LAMMPS_CUSTOM1.java
Atz_DataChangeable.java	JTable_Interaction_LAMMPS_PAIR_COEFF.java
Atz_DataChangeEvent.java	JTable_Interaction_LAMMPS_PAIRS_HARMONIC.java
Atz_DataChangeListener.java	JTable_Interaction_LAMMPS_SPECIAL_BONDS.java
Atz_File_Generator.java	JTable_Interaction_PAIRS_HARMONIC.java
Atz_File_Generator_LAMMPS_USER_SELM1.java	JTable_Lagrangian_ControlPts_BASIC1.java
Atz_FileFilter.java	JTable_Langrangian_CONTROL_PTS.java
Atz_Helper_Generic.java	JTable_MainData.java
Atz_Object_Factory.java	JTable_MainData_XML_LAMMPS_USER_SELM.java
Atz_Object_Factory_Generic.java	JTable_MainData_XML_SELM_Builder.java
Atz_Struct_DataChangeEvent.java	JTable_Preferences_Other.java
Atz_Struct_DataChangeListener.java	JTable_Preferences_Rendering.java
Atz_Struct_DataChangeListener_MainData.java	JTable_Preferences_TableDisplay.java

Features:

Object-oriented classes in Java mirroring parts of SELM.
Dynamic object loaders for delegator design pattern for control flow (extension after compiled byte-codes).
Four main SELM classes correspond to:

- Eulerian Mechanics
- Lagrangian Mechanics
- Fluid-Structure Coupling (Eulerian-Lagrangian communication)
- Time-Step Integration

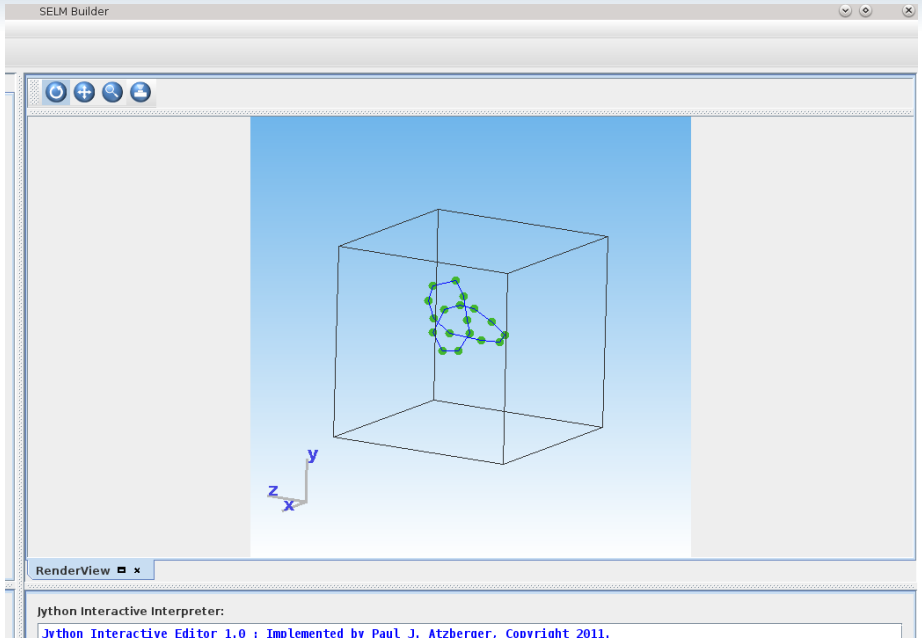
Designed to be easily extended for new types of SELM formulations and integrators.
Custom classes and interfaces for rendering models in 3D and interactively editing models.

Atzberger 2016

Mango Modeling Software

Mango – Codes:

3D Rendering
Atz_LinearAlgebra.java
Atz3D_Camera.java
Atz3D_Element.java
Atz3D_Element_LinePairs.java
Atz3D_Element_Lines.java
Atz3D_Element_Points.java
Atz3D_Element_Points_DataClosest.java
Atz3D_Model.java
Atz3D_Model_SELM.java
Atz3D_Renderer.java
Atz3D_Renderer_SELM.java
JPanel_Model_View_Composite.java
JPanel_Model_View_Composite_XML_SELM_Builder.java
JPanel_Model_View_RenderPanel.java
JPanel_Model_View_RenderPanel_XML_SELM_Builder.java
Physical Units
Atz_Unit.java
Atz_UnitsData.java
Atz_UnitsRef.java
Atz_UnitsRef_PhysicalUnits.java
JDialog_Edit_Units_Ref.java



Features:

Rendering in 3D for interactively editing for model geometry.

Interactive editor features allow for

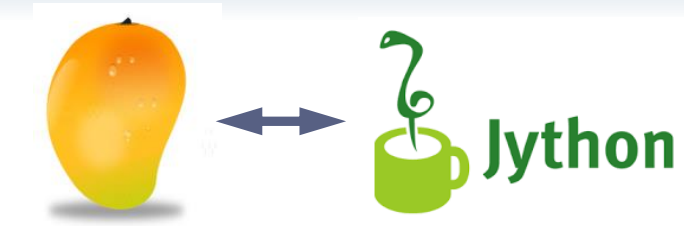
- interactive views of model
- adding / removing control points
- adding / removing bonds between points
- adding custom force interactions

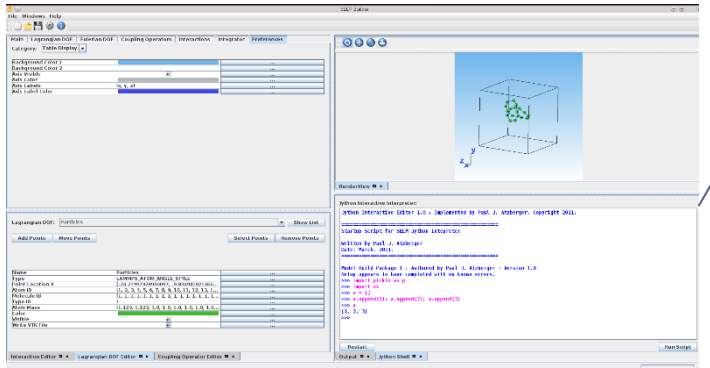
Custom classes implemented for tracking physical units in tables.

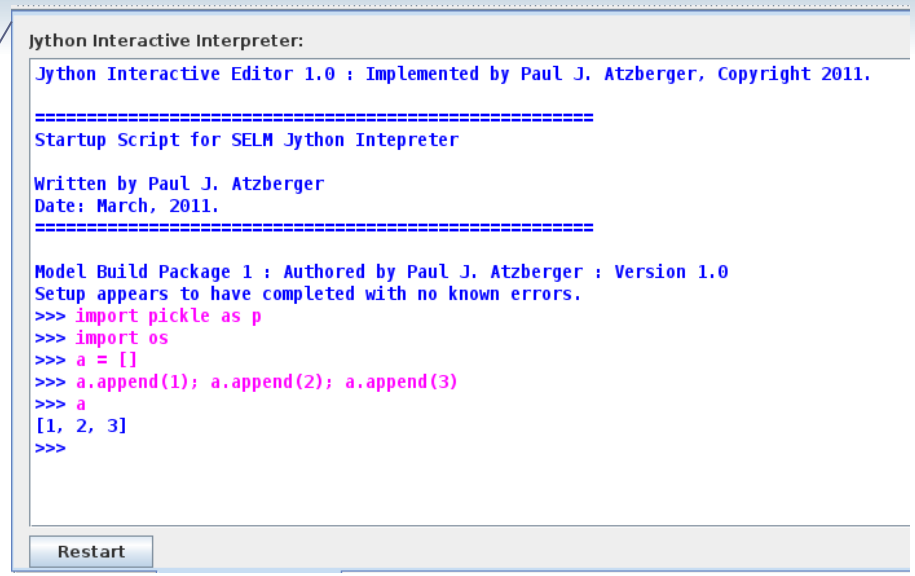
Atzberger 2016

Mango GUI Jython Interface

MANGO - Modeling Software:





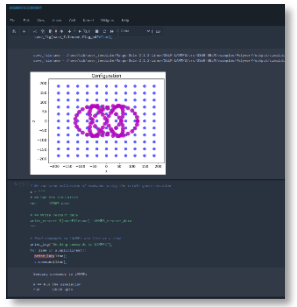


Jython Terminal:

Custom classes implement interactive terminal based on Jython.
Wrapper jython classes implemented for MANGO interface and SELM data structures.
Editor features allow for

- jython/python scripting to construct models
- custom GUI windows : interactive components in MANGO
- post-processing scripts
- generation of SELM XML files from the constructed MANGO data structures.

Python and Jupyter notebook interfaces



Jupyter notebooks and Python interface now also available (directly with Selm-Lammps library).

Atzberger 2016

Selm-Lammps Integration

Python and Jupyter Notebook Interfaces

Tips for SELM Package: Installation and Usage

Instructions

Pre-compiled binaries: for (Debian 9+/Ubuntu and Centos 7+, Python 3.6+).

Quick start:
>> pip install selm-lammps
test: >> python -c "from selm_lammps.tests import t1; t1.test()“

Alternatively, can use *docker run -it ubuntu:20.04 /bin/bash; (use python3).*

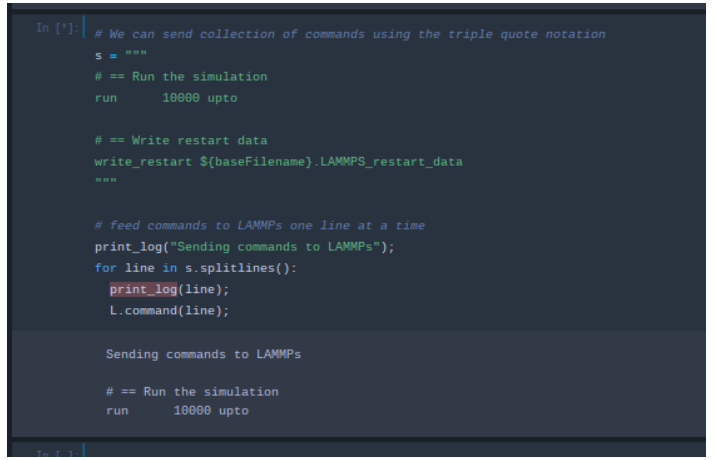
Examples, docs, source: see http://mango-selm.org/

Directories:
- src/USER-SELM: main C/C++ interface codes for SELM package
- examples/USER/selm: example models and simulation scripts
- lib/selm: library of SELM integrators and related algorithms

Installing Python components (uses lammps.py, lammps.so):
- Recommended to use *conda* or *virtualenv* with python >=3.6
- Examples for Jupyter notebooks, python scripts, for running simulations.
- See README files for more details.

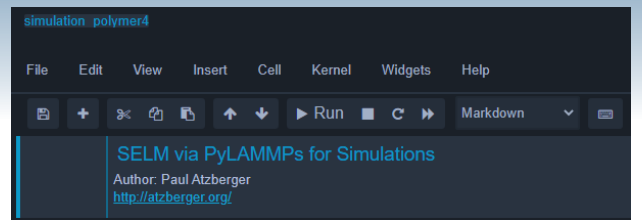
Jupyter Notebooks and Python-based Simulations:
- Uses python-interfaces to LAMMPs.
- L.command(cmd_str); runs the command in cmd_str.
- Model building using python wrapper
  - sets up particles
  - sets up interactions, many possible types and potential available
  - sets up the simulation parameters.

Python and Jupyter notebook interfaces

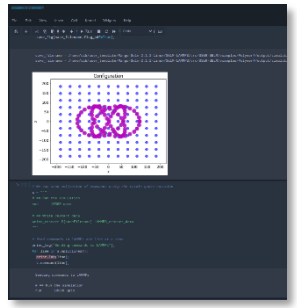


Jupyter Notebook and Python Interface

Python Jupyter Notebook



Python and Jupyter notebook interfaces



Create Selm-Lammps instance

```
Setup LAMMPs

In [10]: L = IPyLammps()
         print_version_info();

LAMMPS output is captured by PyLammps wrapper
LAMMPS version: 29 Oct 2020 / 20201029
MPI version: LAMMPS MPI STUBS for LAMMPS version 29 Oct 2020
```

Issuing commands

```
In [ ]: cmd_str = "lammps_command"
        L.command(cmd_str);
```

Setup model geometry and interactions

```
Setup the Simulation Files (such as .read_data)

In [13]: num_dim = 3;
         box = np.zeros((num_dim,2));
         LL = 202.5; box[:,0] = -LL; box[:,1] = LL;

         # setup atoms
         I_id = 1; I_type = 1; atom_types = [];
         atom_list = []; atom_mass_list = []; atom_id_list = [];
         atom_mol_list = []; atom_name_list = [];

         # polymer atoms
         atom_name = "polymer_pts";
         atom_name_list.append(atom_name);
         atom_types.append(I_type);
```

```
num_pts = 100;
t = np.linspace(0,2*np.pi,num_pts); R0 = 40;
x1 = R0*(2.0 + np.cos(2.0*t))*np.cos(3.0*t);
x2 = R0*(2.0 + np.cos(2.0*t))*np.sin(3.0*t);
x3 = R0*2*np.sin(4.0*t);
x = np.stack((x1,x2,x3),axis=1); # shape = [num_pts,num_dim]
num_pts = x.shape[0]; m0 = 1.123;
```

Model configuration (generated file)

```
# ================================================================================
# LAMMPS file for 'read_data' command
#
# Generated by selm python scripts by Paul J. Atzberger.
#
# ================================================================================

# ================================================================================
# Description:
# --------------------------------------------------------------------------------
#
# SELM_Lagrangian = SELM_Lagrangian_LAMMPS_ATOM_ANGLE_STYLE
# LagrangianName = Points
# LagrangianTypeStr = LAMMPS_ATOM_ANGLE_STYLE
#
# SELM_Eulerian   = SELM_Eulerian_LAMMPS_SHEAR_UNIFORM1_FFTW3
#
# atom_type = angle_type
#
# ================================================================================

# ================================================================================
# Header information:
# --------------------------------------------------------------------------------
1431 atoms
99 bonds
98 angles

2 atom types
1 bond types
1 angle types
# ================================================================================

# ================================================================================
# Domain Size Specification:
# --------------------------------------------------------------------------------
-202 202 xlo xhi
-202 202 ylo yhi
```

Setup parameters

```
# We can send collection of commands using the triple quote notation
s = """
# ================================================================================
# LAMMPS main parameter file and script
#
# Author: Paul J. Atzberger.
#
# Based on script generated by MANGO-SELM Model Builder.
#
# ================================================================================

# == Setup variables for the script

variable dumpfreq         equal    1
variable restart          equal    0
variable neighborSkinDist equal    1.0 # distance for bins beyond force cut-off (1.0 + 1.0
variable baseFilename     universe Polymer

# == Setup the log file
#log         ${baseFilename}.LAMMPS_logFile

# == Setup style of the run

# type of units to use in the simulation (units used are in fact: amu, nm, ns, Kelvins)
units       real

# indicates possible types allowed for interactions between the atoms
atom_style  angle

# indicates possible types allowed for bonds between the atoms
#bond_style  hybrid fene
```

SELM XML files

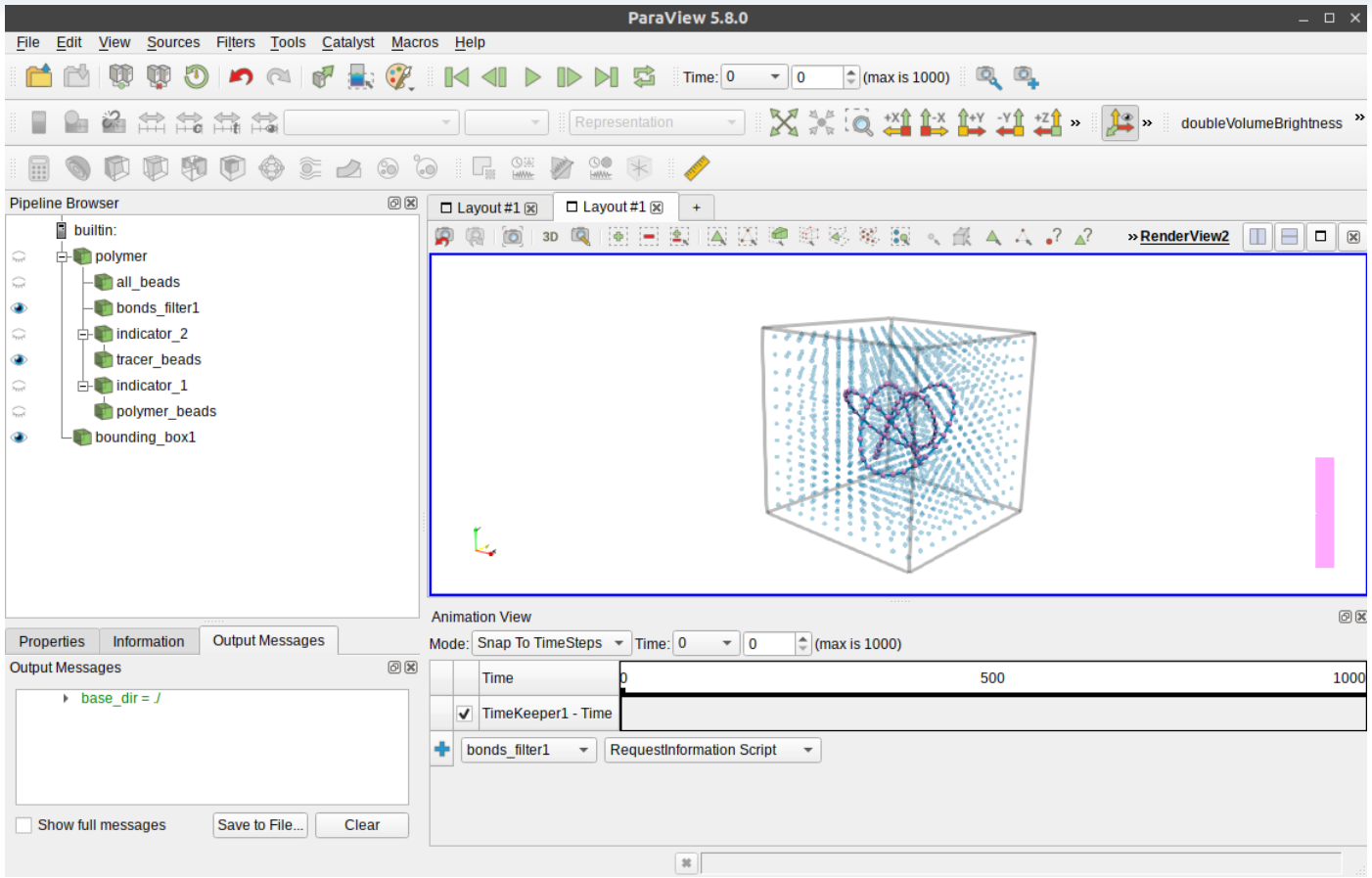
Run simulation and analysis

```
In [20]: # We can send collection of commands using the triple quote notation
         s = """
         # == Run the simulation
         run      1000 upto

         # == Write restart data
         write_restart ${baseFilename}.LAMMPS_restart_data
         """

         # feed commands to LAMMPs one line at a time
         print_log("Sending commands to LAMMPs");
         for line in s.splitlines():
           print_log(line);
           L.command(line);
```

Interface allows for:

- checking intermediate results
- resuming simulations
- perform analysis and visualization.

Paraview for Visualization



Features:

- Processing VTK data output files (.vtp, .vtu, .vtr)
- Selm python scripts for loading and visualizing models.
- Rendering capabilities and movie generation.
- Analysis capabilities for statistics and other model properties.

How to Setup Model in Practice

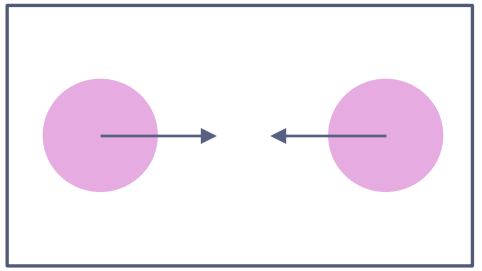
Examples

Particles: Thermal Fluctuations with Hydrodynamic Correlations

Directory:
examples/hydro1

Jupyter notebook:
simulation_hydro1.ipynb

particles w/ hydrodynamics



SELM via PyLAMMPs for Simulations

Author: Paul Atzberger
http://atzberger.org/

```
import os;
script_base_name = "simulation_particles1";
script_dir = os.getcwd();
```

```
# import the lammps module
try:
  from selm_lammps.lammps import IPyLammps # use this for the pip install of pre-built package
  lammps_import_comment = "from selm_lammps.lammps import IPyLammps";
  from selm_lammps import util as atz_util;
except Exception as e:
  from lammps import IPyLammps # use this for direct install of package
  lammps_import_comment = "from lammps import IPyLammps";
  from atz_lammps import util as atz_util;
except Exception as e: # if fails to import, report the exception
  print(e);
  lammps_import_comment = "import failed";
```

Setup LAMMPs

```
L = IPyLammps();
atz_util.print_version_info(L);
```

```
LAMMPS output is captured by PyLammps wrapper
LAMMPS version: 29 Oct 2020 / 20201029
MPI version: LAMMPS MPI STUBS for LAMMPS version 29 Oct 2020
```

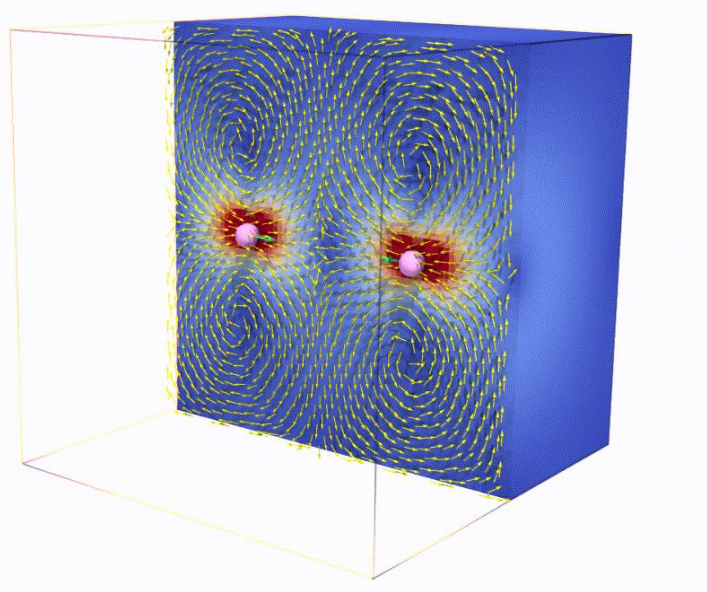
Setup the Model and Simulation Files (such as .read_data)

```
num_dim = 3;
box = np.zeros((num_dim,2));
LL = 202.5; box[:,0] = -LL; box[:,1] = LL;

# setup atoms
I_id = 1; I_type = 1; atom_types = [];
atom_list = []; atom_mass_list = []; atom_id_list = [];
atom_mol_list = []; atom_name_list = [];
```

Perform the simulation

```
# == Setup the SELM integrator
fix 1 all selm Main.SELM_params
```

```
# feed commands to LAMMPs one line at a time
print_log("Sending commands to LAMMPs");
for line in s.splitlines():
  print_log(line);
  L.command(line);
```

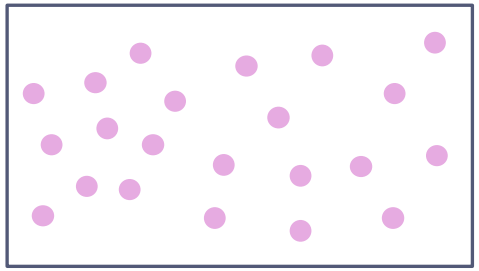


Particles: Thermal Fluctuations with Hydrodynamic Correlations

Directory:
examples/particles1

Jupyter notebook:
simulation_particles1.ipynb

particle diffusion w/
hydrodynamic correlations



SELM via PyLAMMPs for Simulations

Author: Paul Atzberger
http://atzberger.org/

```
import os;
script_base_name = "simulation_particles1";
script_dir = os.getcwd();
```

```
# import the lammps module
try:
  from selm_lammps.lammps import IPyLammps # use this for the pip install of pre-built package
  lammps_import_comment = "from selm_lammps.lammps import IPyLammps";
  from selm_lammps import util as atz_util;
except Exception as e:
  from lammps import IPyLammps # use this for direct install of package
  lammps_import_comment = "from lammps import IPyLammps";
  from atz_lammps import util as atz_util;
except Exception as e: # if fails to import, report the exception
  print(e);
  lammps_import_comment = "import failed";
```

Setup LAMMPs

```
L = IPyLammps();
atz_util.print_version_info(L);
```

```
LAMMPS output is captured by PyLammps wrapper
LAMMPS version: 29 Oct 2020 / 20201029
MPI version: LAMMPS MPI STUBS for LAMMPS version 29 Oct 2020
```

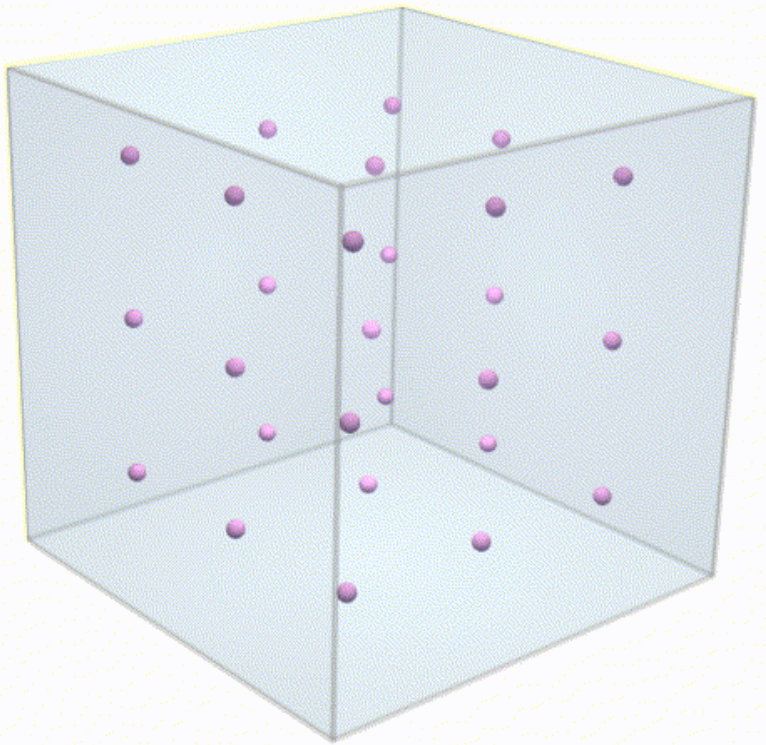
Setup the Model and Simulation Files (such as .read_data)

```
num_dim = 3;
box = np.zeros((num_dim,2));
LL = 202.5; box[:,0] = -LL; box[:,1] = LL;

# setup atoms
I_id = 1; I_type = 1; atom_types = [];
atom_list = []; atom_mass_list = []; atom_id_list = [];
atom_mol_list = []; atom_name_list = [];
```

Perform the simulation

```
# == Setup the SELM integrator
fix 1 all selm Main.SELM_params
```

```
# feed commands to LAMMPs one line at a time
print_log("Sending commands to LAMMPs");
for line in s.splitlines():
  print_log(line);
  L.command(line);
```



Polymer: Thermal Fluctuations with Hydrodynamic Correlations

Directory:
examples/polymer4

Jupyter notebook:
simulation_polymer4.ipynb

Create Selm-Lammps instance

Setup LAMMPs

In [10]:
```
L = IPyLammps()
print_version_info();
```

```
LAMMPS output is captured by PyLammps wrapper
LAMMPS version: 29 Oct 2020 / 20201029
MPI version: LAMMPS MPI STUBS for LAMMPS version 29 Oct 2020
```

Setup model geometry and interactions

Setup the Simulation Files (such as .read_data)

In [13]:
```
num_dim = 3;
box = np.zeros((num_dim,2));
LL = 202.5; box[:,0] = -LL; box[:,1] = LL;

# setup atoms
I_id = 1; I_type = 1; atom_types = [];
atom_list = []; atom_mass_list = []; atom_id_list = [];
atom_mol_list = []; atom_name_list = [];

# polymer atoms
atom_name = "polymer_pts";
atom_name_list.append(atom_name);
atom_types.append(I_type);
```

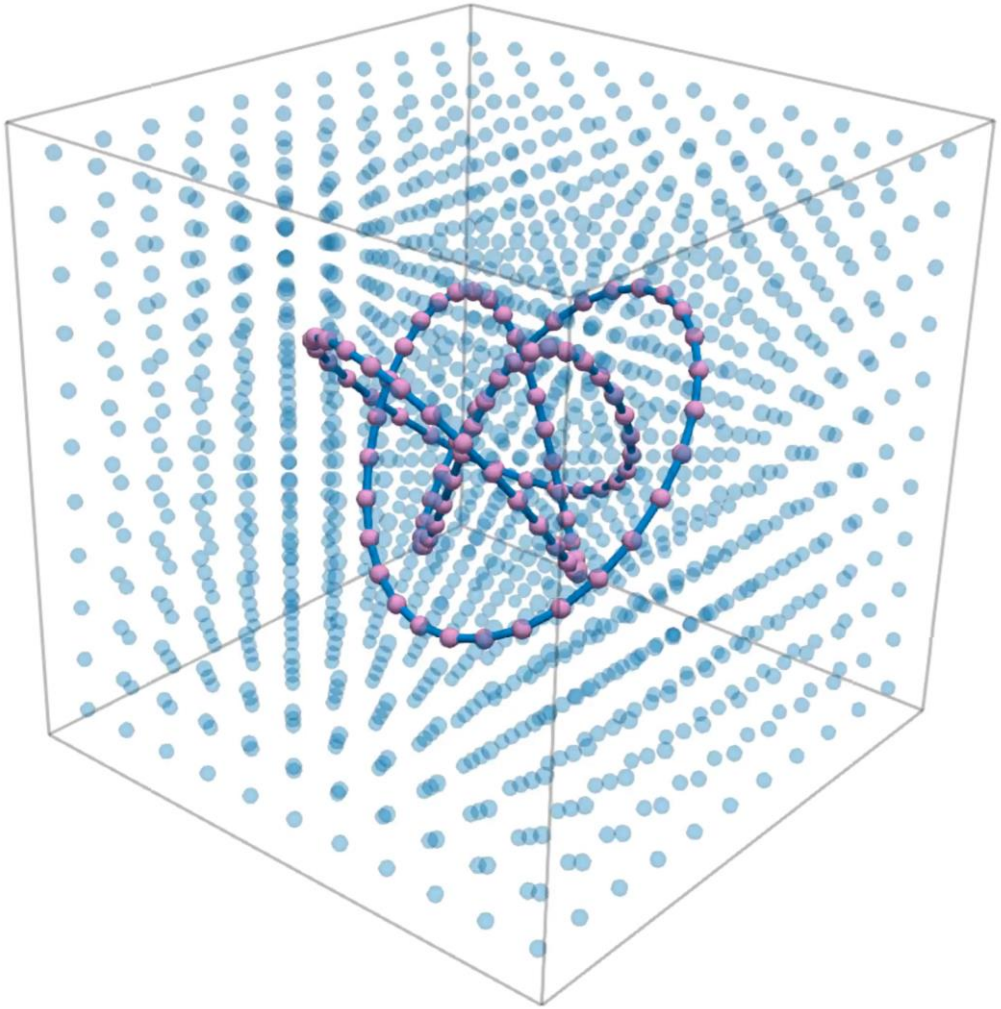
```
num_pts = 100;
t = np.linspace(0,2*np.pi,num_pts); R0 = 40;
x1 = R0*(2.0 + np.cos(2.0*t))*np.cos(3.0*t);
x2 = R0*(2.0 + np.cos(2.0*t))*np.sin(3.0*t);
x3 = R0*2*np.sin(4.0*t);
x = np.stack((x1,x2,x3),axis=1); # shape = [num_pts,num_dim]
num_pts = x.shape[0]; m0 = 1.123;
```

Run simulation and analysis

In [20]:
```
# We can send collection of commands using the triple quote notation
s = """
# == Run the simulation
run      1000 upto

# == Write restart data
write_restart ${baseFilename}.LAMMPS_restart_data
"""

# feed commands to LAMMPs one line at a time
print_log("Sending commands to LAMMPs");
for line in s.splitlines():
  print_log(line);
  L.command(line);
```

SELM XML files

Polymer knot fluctuations w/ hydrodynamic correlations



Polymer Knot: Subject to Shearing and Thermal Fluctuations

Directory:
examples/polymer4

Jupyter notebook:
simulation_polymer4.ipynb

Create Selm-Lammps instance

```
Setup LAMMPs

In [10]:
L = IPyLammps()
print_version_info();

  LAMMPS output is captured by PyLammps wrapper
  LAMMPS version: 29 Oct 2020 / 20201029
  MPI version: LAMMPS MPI STUBS for LAMMPS version 29 Oct 2020
```

Setup model geometry and interactions

```
Setup the Simulation Files (such as .read_data)

In [13]:
num_dim = 3;
box = np.zeros((num_dim,2));
LL = 202.5; box[:,0] = -LL; box[:,1] = LL;

# setup atoms
I_id = 1; I_type = 1; atom_types = [];
atom_list = []; atom_mass_list = []; atom_id_list = [];
atom_mol_list = []; atom_name_list = [];

# polymer atoms
atom_name = "polymer_pts";
atom_name_list.append(atom_name);
atom_types.append(I_type);
```

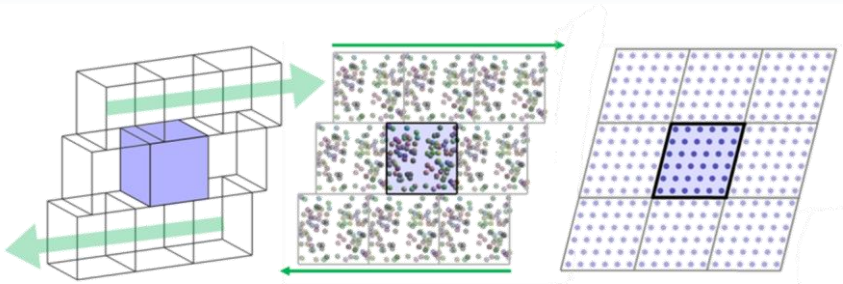
```
num_pts = 100;
t = np.linspace(0,2*np.pi,num_pts); R0 = 40;
x1 = R0*(2.0 + np.cos(2.0*t))*np.cos(3.0*t);
x2 = R0*(2.0 + np.cos(2.0*t))*np.sin(3.0*t);
x3 = R0*2*np.sin(4.0*t);
x = np.stack((x1,x2,x3),axis=1); # shape = [num_pts,num_dim]
num_pts = x.shape[0]; m0 = 1.123;
```

Run simulation and analysis

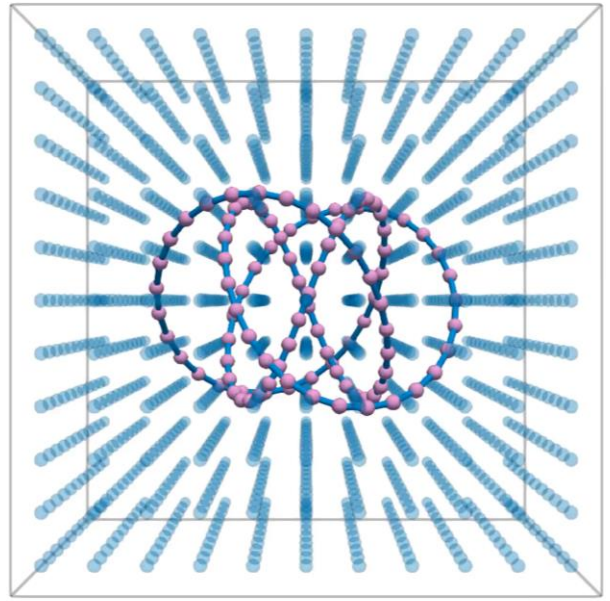
```
In [20]:
# We can send collection of commands using the triple quote notation
s = """
# == Run the simulation
run      1000 upto

# == Write restart data
write_restart ${baseFilename}.LAMMPS_restart_data
"""

# feed commands to LAMMPs one line at a time
print_log("Sending commands to LAMMPs");
for line in s.splitlines():
  print_log(line);
  L.command(line);
```

SELM XML files

Shearing boundaries: Less-Edwards conditions

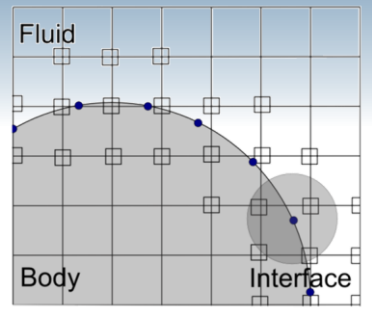


Polymer knot fluctuations in shear flow

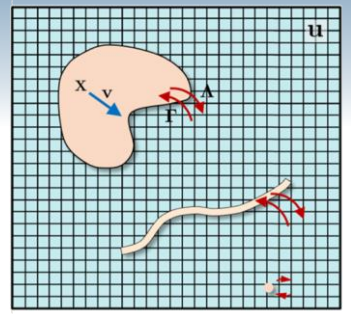


Further Simulations with SELMs

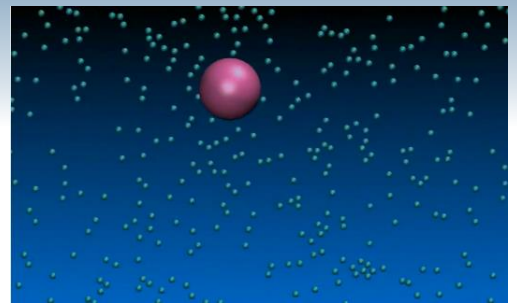
SELM Fluctuating Hydrodynamics

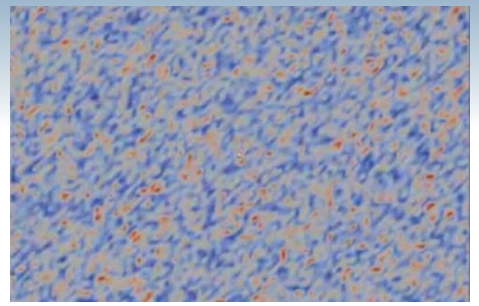


Eulerian-Lagrangian Mechanics



Eulerian-Lagrangian Coupling


Brownian Motion: Molecular Collisions


Continuum Gaussian Random Field

SELM Inertial Regime I:

hydrodynamics

$$\begin{aligned} \rho\frac{\partial \mathbf{u}}{\partial t} &= \mu\Delta\mathbf{u} - \nabla p + \Lambda[\Upsilon(\mathbf{v}-\Gamma\mathbf{u})] + \mathbf{f}_{thm} \\ \nabla\cdot\mathbf{u} &= 0. \end{aligned}$$

microstructure

$$\begin{aligned} \frac{d\mathbf{X}}{dt} &= \mathbf{v} \\ m\frac{d\mathbf{v}}{dt} &= -\Upsilon(\mathbf{v}-\Gamma\mathbf{u}) - \nabla_X\Phi[X] + \mathbf{F}_{thm}. \end{aligned}$$

thermal fluctuations

$$\begin{aligned} \langle \mathbf{f}_{\text{thm}}(s)\mathbf{f}^T_{\text{thm}}(t)\rangle &= -(2k_BT)\,(\mathcal{L}-\Lambda\Upsilon\Gamma)\,\delta(t-s) \\ \langle \mathbf{F}_{\text{thm}}(s)\mathbf{F}^T_{\text{thm}}(t)\rangle &= (2k_BT)\,\Upsilon\,\delta(t-s) \\ \langle \mathbf{f}_{\text{thm}}(s)\mathbf{F}^T_{\text{thm}}(t)\rangle &= -(2k_BT)\,\Lambda\Upsilon\,\delta(t-s). \end{aligned}$$

SELM Overdamped Regime IV:

microstructure + hydrodynamics (quasi-steady)

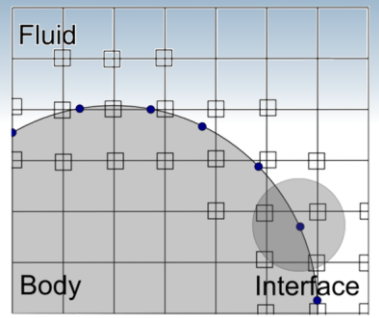
$$\begin{aligned} \frac{d\mathbf{X}}{dt} &= H_{\text{SELM}}[-\nabla_{\mathbf{X}}\Phi(\mathbf{X})] \\ &+ (\nabla_{\mathbf{X}}\cdot H_{\text{SELM}})k_BT + \mathbf{h}_{\text{thm}} \\ H_{\text{SELM}} &= \Gamma(-\wp\mathcal{L})^{-1}\Lambda \end{aligned}$$

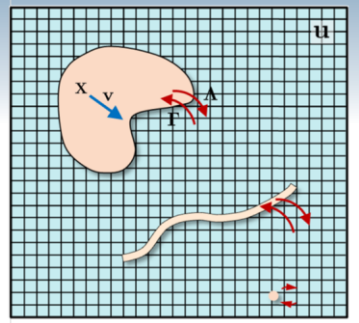
thermal fluctuations

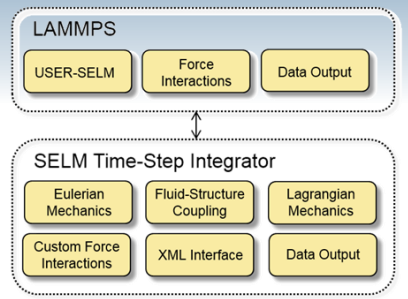
$$\langle \mathbf{h}_{\text{thm}}(s)\mathbf{h}^T_{\text{thm}}(t)\rangle = (2k_BT)\,H_{\text{SELM}}\,\delta(t-s).$$

Atzberger 2015

MANGO-SELM Simulation Software







SELM Inertial Regime I (Verlet-stye temporal integration):

microstructure

$$\begin{aligned}\mathbf{v}^{n+\frac{1}{2}} &= \mathbf{v}^{n} + \frac{\Delta t}{2} m^{-1}\mathbf{F}^{n} \\ &+ \frac{\Delta t}{2}\left(-m^{-1}\Upsilon\left(\mathbf{v}^{n-\frac{1}{2}} - \Gamma^{n}\mathbf{u}^{n-\frac{1}{2}}\right)\right. \\ &\left. + m^{-1}\mathbf{g}^{n-\frac{1}{2}}\right) \\ \mathbf{X}^{n+1} &= \mathbf{X}^{n} + \mathbf{v}^{n+\frac{1}{2}}\Delta t\end{aligned}$$

hydrodynamics

$$\begin{aligned}\mathbf{u}^{n+\frac{1}{2}} &= \mathbf{u}^{n} + \frac{\Delta t}{2}\rho^{-1}\mu L\mathbf{u}^{n-\frac{1}{2}} \\ &- \frac{\Delta t}{2}\left(\rho^{-1}\Lambda^{n}\left[-\Upsilon\left(\mathbf{v}^{n-\frac{1}{2}} - \Gamma^{n}\mathbf{u}^{n-\frac{1}{2}}\right)\right.\right. \\ &\left.\left. + \mathbf{g}^{n-\frac{1}{2}}\right]\right) \\ &+ \mathbf{h}^{n-\frac{1}{2}}\end{aligned}$$

thermal fluctuations

$$\begin{aligned}\langle \mathbf{g}^{n-\frac{1}{2}}\mathbf{g}^{n-\frac{1}{2}T}\rangle &= 4k_B T\Upsilon/\Delta t \\ \langle \mathbf{h}^{n}\mathbf{h}^{nT}\rangle &= 4k_B T\rho^{-2}\mu L/\Delta t.\end{aligned}$$

microstructure

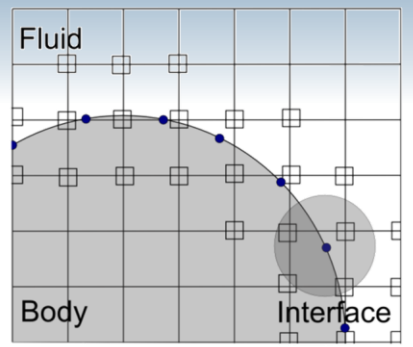
$$\begin{aligned}\mathbf{v}^{n+1} &= \mathbf{v}^{n+\frac{1}{2}} + \frac{\Delta t}{2} m^{-1}\mathbf{F}^{n+1} \\ &+ \frac{\Delta t}{2}\left(-m^{-1}\Upsilon\left(\mathbf{v}^{n+\frac{1}{2}} - \Gamma^{n+1}\mathbf{u}^{n+\frac{1}{2}}\right)\right. \\ &\left. + m^{-1}\mathbf{g}^{n+\frac{1}{2}}\right)\end{aligned}$$

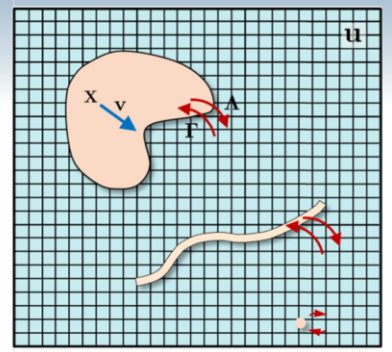
hydrodynamics

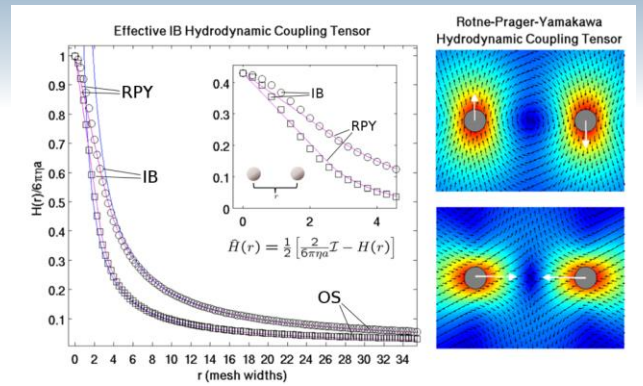
$$\begin{aligned}\mathbf{u}^{n+1} &= \mathbf{u}^{n+\frac{1}{2}} + \frac{\Delta t}{2}\rho^{-1}\mu L\mathbf{u}^{n+\frac{1}{2}} \\ &- \frac{\Delta t}{2}\left(\rho^{-1}\Lambda^{n+1}\left[-\Upsilon\left(\mathbf{v}^{n+\frac{1}{2}} - \Gamma^{n+1}\mathbf{u}^{n+\frac{1}{2}}\right)\right.\right. \\ &\left.\left. + \mathbf{g}^{n+\frac{1}{2}}\right]\right) \\ &+ \mathbf{h}^{n+\frac{1}{2}}.\end{aligned}$$

Atzberger 2015

MANGO-SELM Simulation Software







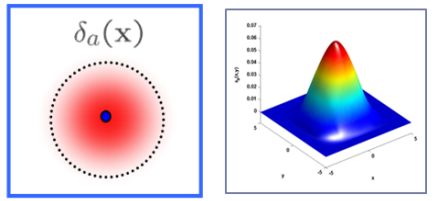
SELM Coupling:

adjoint condition

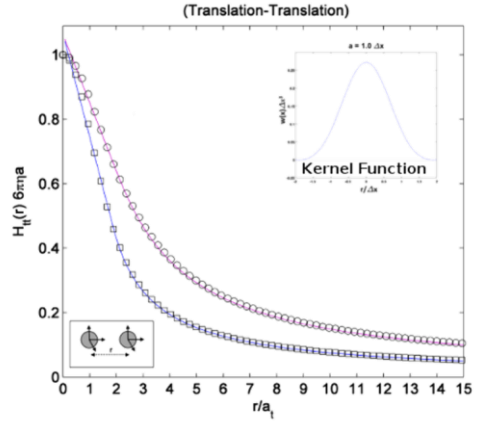
$$\langle \Gamma \mathbf{v}, \mathbf{F} \rangle \;=\; \sum_i [\Gamma \mathbf{v}]_i \cdot [\mathbf{F}]_i \;=\; \int_\Omega \mathbf{v}(\mathbf{x}) \cdot (\Lambda \mathbf{F})(\mathbf{x}) d\mathbf{x} \;=\; \langle \mathbf{v}, \Lambda \mathbf{F} \rangle$$

IB-Kernel coupling:

$$\begin{aligned} \Gamma \mathbf{u} &= \int_\Omega \eta(\mathbf{y} - \mathbf{X}(t))\, \mathbf{u}(\mathbf{y}, t) d\mathbf{y} \\ \Lambda \mathbf{F} &= \eta(\mathbf{x} - \mathbf{X}(t))\, \mathbf{F}. \end{aligned}$$



Peskin delta-function



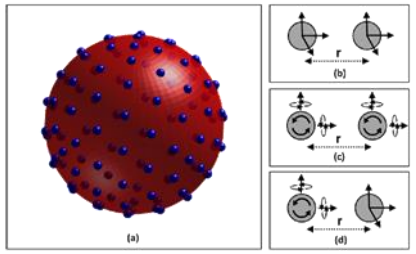
Generalized Coupling (Faxen)

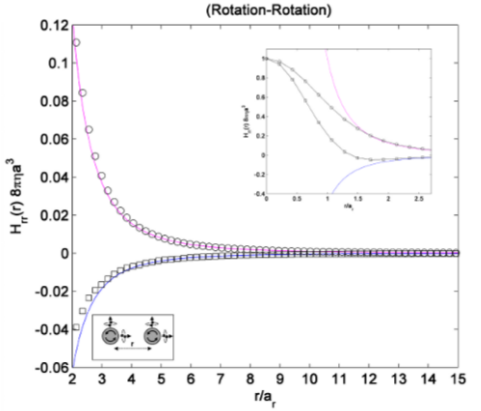
$$\Gamma_0 \mathbf{u} = \sum_{\mathbf{m}} \left\langle\, \eta_0(\mathbf{y_m} - (\mathbf{X}_{\rm cm} + \mathbf{z}))\; \mathbf{u_m} \,\right\rangle_{\tilde{\mathcal{S}}, |\mathbf{z}| = R} \Delta x^3_{\mathbf{m}}$$

$$\Gamma_1 \mathbf{u} = \frac{3}{2R^2} \sum_{\mathbf{m}} \left\langle\, \eta_1(\mathbf{y_m} - (\mathbf{X}_{\rm cm} + \mathbf{z}))\, (\mathbf{z} \times \mathbf{u_m}) \,\right\rangle_{\tilde{\mathcal{S}}, |\mathbf{z}| = R} \Delta x^3_{\mathbf{m}}.$$

$$\Lambda_0(\mathbf{x_m}) = \left(\left\langle\, \eta_0(\mathbf{x_m} - (\mathbf{X}_{\rm cm} + \mathbf{z})) \,\right\rangle_{\tilde{\mathcal{S}}, |\mathbf{z}| = R} \right) \mathbf{F}$$

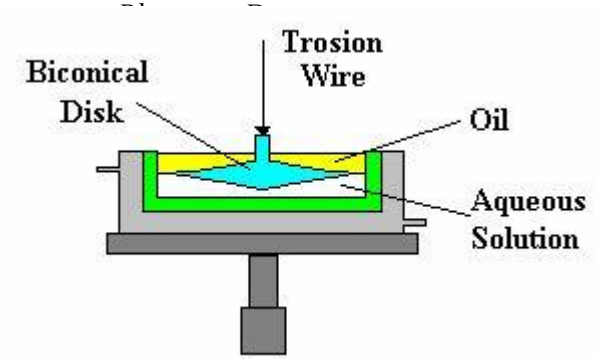
$$\Lambda_1(\mathbf{x_m}) = -\frac{3}{2R^2} \left(\left\langle\, \mathbf{z} \eta_1(\mathbf{x_m} - (\mathbf{X}_{\rm cm} + \mathbf{z})) \,\right\rangle_{\tilde{\mathcal{S}}, |\mathbf{z}| = R} \right) \times \mathbf{T}.$$

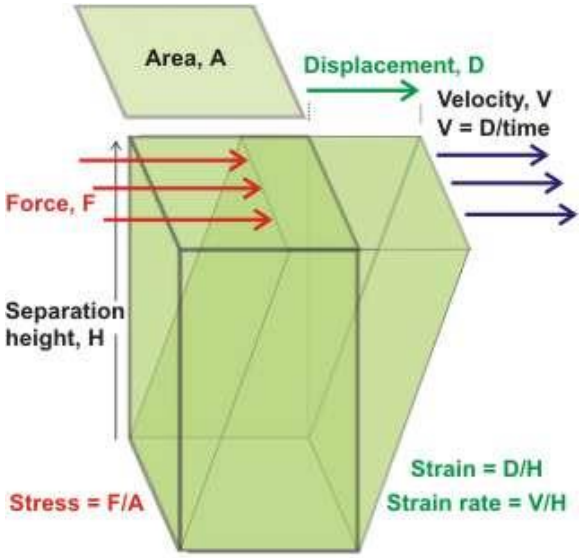




Atzberger 2011, Atzberger 2015

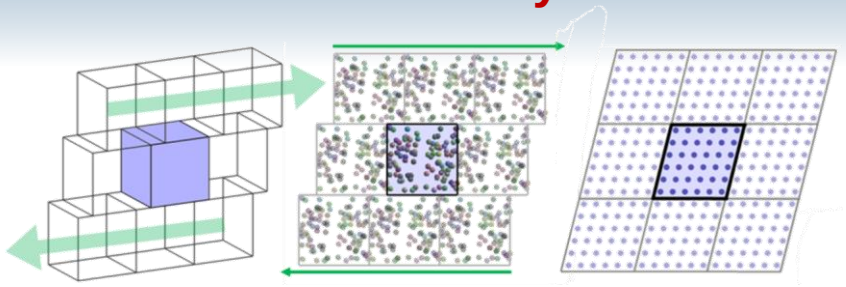
Rheological Properties and Microstructure Dynamics



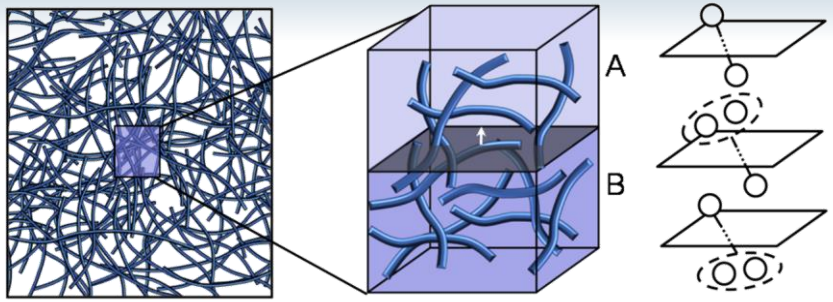


MANGO-SELM Simulation Software

Lees-Edwards Boundary Conditions:



Material Stress ←Microscopic Forces



Stress Tensor Estimator:

$$\sigma_{\ell,z}^{(n)} = \frac{1}{AL} \sum_{\mathbf{q}\in\mathcal{Q}_n} \sum_{j=1}^{n-1} \left\langle \mathbf{f}_{\mathbf{q},j}^{(\ell)} \cdot \left(\mathbf{x}_{q_n}^{*,(z)} - \mathbf{x}_{q_j}^{*,(z)} \right) \right\rangle$$

Fluctuating hydrodynamics (moving frame):

$$\begin{aligned}
\rho \frac{d\mathbf{w}}{dt} &= L(t)\mathbf{w} + \lambda + \Lambda[-\nabla_{\mathbf{X}}\Phi] + (\nabla_{\mathbf{X}} \cdot \Lambda)\, k_B T + \mathbf{J} + \mathbf{h}_{\text{thm}} \\
S(t)\cdot\mathbf{w} &= \mathbf{K} \\
\frac{d\mathbf{X}}{dt} &= \Gamma\mathbf{w}.
\end{aligned}$$

$$\begin{aligned}
S(t)\cdot\mathbf{w} &= D\cdot\mathbf{w} + \mathbf{e}_z^T\, G\mathbf{w}\, \mathbf{e}_x \dot{\gamma} t \\
L(t)\mathbf{w} &= \mu \left[\mathbf{e}_d - \delta_{d,3}\dot{\gamma} t \mathbf{e}_x\right]^T A\mathbf{w} \left[\mathbf{e}_d - \delta_{d,3}\dot{\gamma} t \mathbf{e}_x\right]
\end{aligned}$$

$$\begin{aligned}
G(s,t) &= \langle \mathbf{h}_{\text{thm}}(s)\mathbf{h}_{\text{thm}}(t)^T \rangle \\
G(s,t) &= -2\wp(t)L(t)C\delta(t-s)
\end{aligned}$$

$$D\cdot\mathbf{w} = \sum_{d=1}^{3} \frac{\mathbf{w}^{(d)}(\mathbf{q}+\mathbf{e}_d) - \mathbf{w}^{(d)}(\mathbf{q}-\mathbf{e}_d)}{2\Delta x}$$

$$[G\mathbf{w}]_{ij} = \frac{\mathbf{w}^{(i)}(\mathbf{q}+\mathbf{e}_j) - \mathbf{w}^{(i)}(\mathbf{q}-\mathbf{e}_j)}{2\Delta x}$$

$$\begin{aligned}
[A\mathbf{w}]_{ii} &= \frac{\mathbf{w}^{(i)}(\mathbf{q}+\mathbf{e}_i) - 2\mathbf{w}^{(i)}(\mathbf{q}) + \mathbf{w}^{(i)}(\mathbf{q}-\mathbf{e}_i)}{\Delta x^2} \\
[A\mathbf{w}]_{ij} &= \frac{\mathbf{w}^{(d)}(\mathbf{q}+\mathbf{e}_i+\mathbf{e}_j) - \mathbf{w}^{(d)}(\mathbf{q}-\mathbf{e}_i+\mathbf{e}_j)}{4\Delta x^2} \\
&\quad - \frac{\mathbf{w}^{(d)}(\mathbf{q}+\mathbf{e}_i-\mathbf{e}_j) - \mathbf{w}^{(d)}(\mathbf{q}-\mathbf{e}_i-\mathbf{e}_j)}{4\Delta x^2}, \quad i \neq j.
\end{aligned}$$

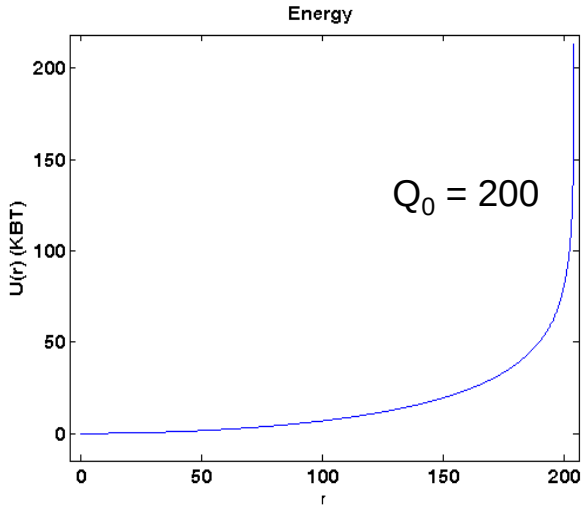
Atzberger 2013

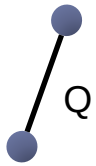
MANGO-SELM Simulation Software

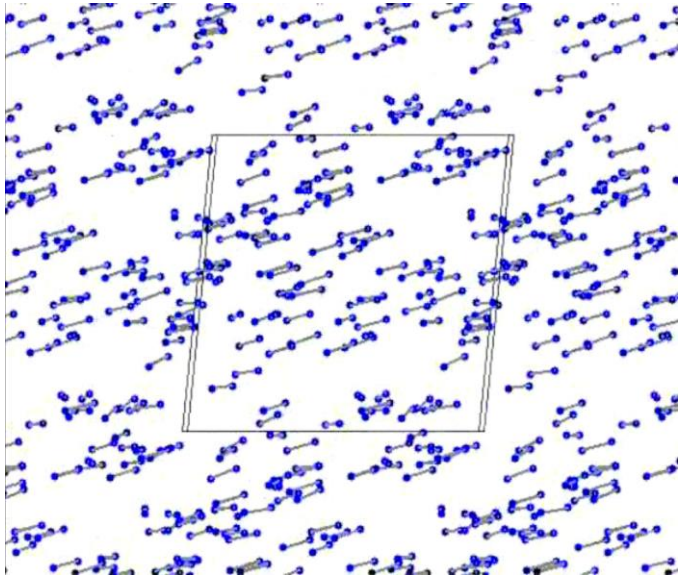
Example System : Finitely Extensible Nonlinear Elastic (FENE) Dimers:

Potential Energy:

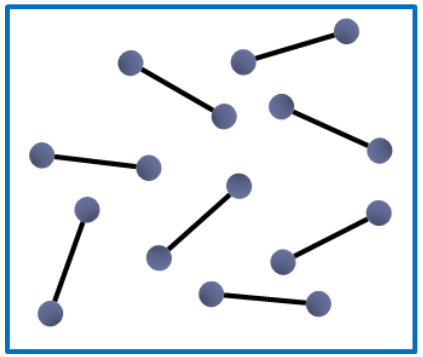
$$U(r) = -\frac{K}{2} Q_0^2 \log(1 - (Q/Q_0)^2)$$



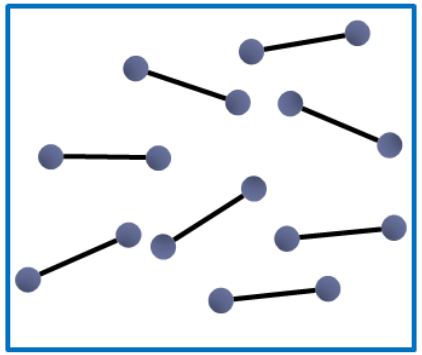




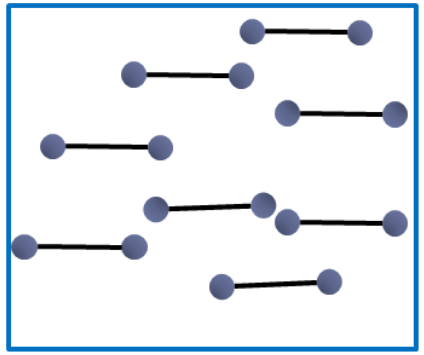
low shear rate



medium shear rate

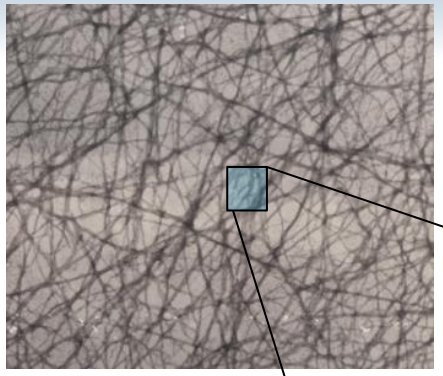


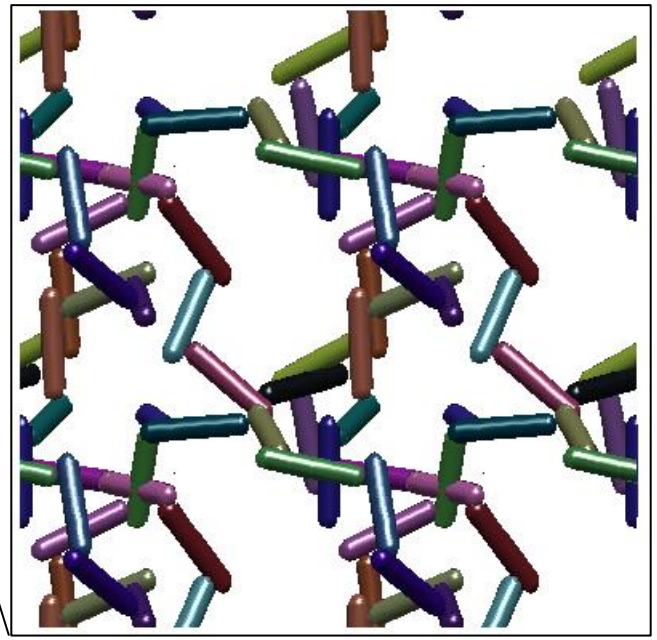
large shear rate



Atzberger 2013

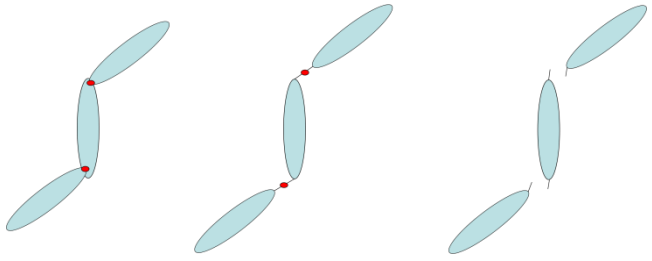
Gel-like Materials



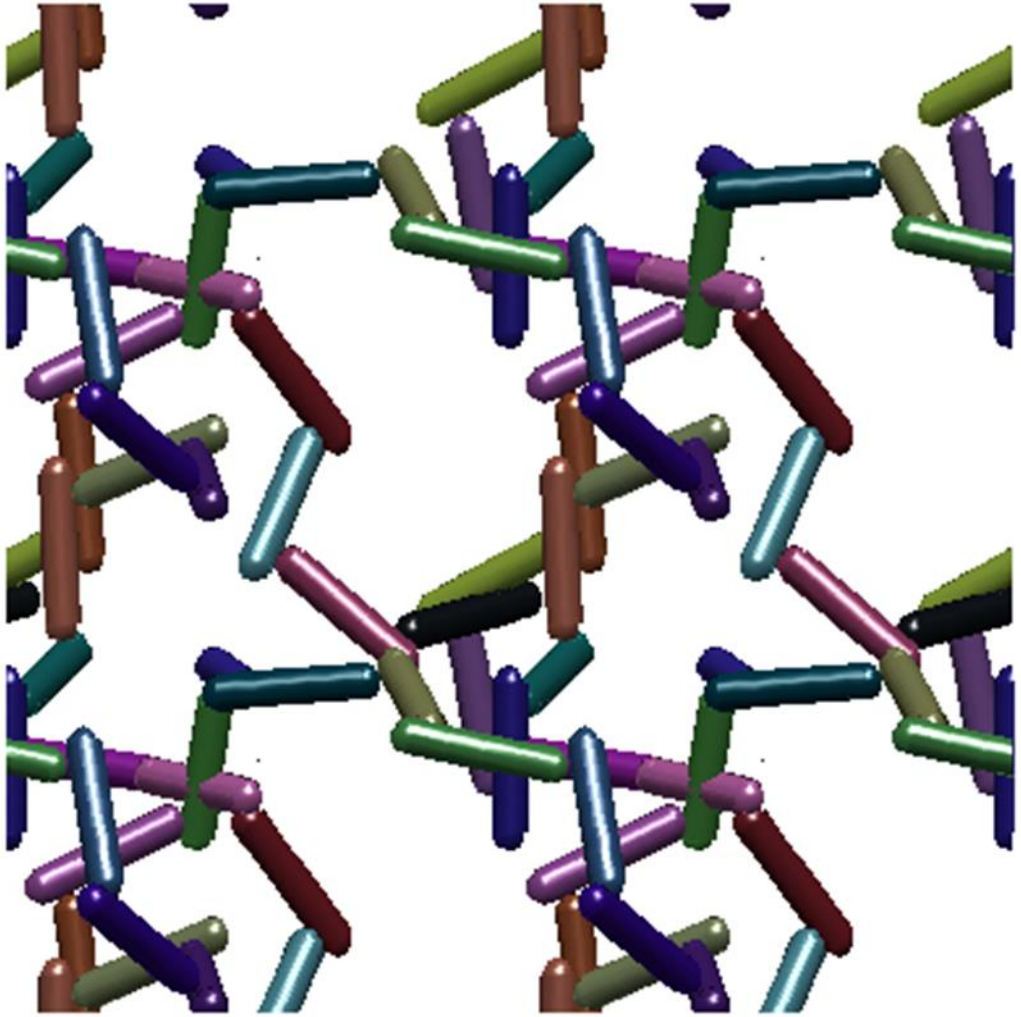


Polymeric Gel Model:

- Worm-like chain elasticity for individual polymers.
- Near-end segments “sticky”.
- Branches bond angles are 70 degrees.
- Yield of “sticky” ends after 50% rest-length stretchi

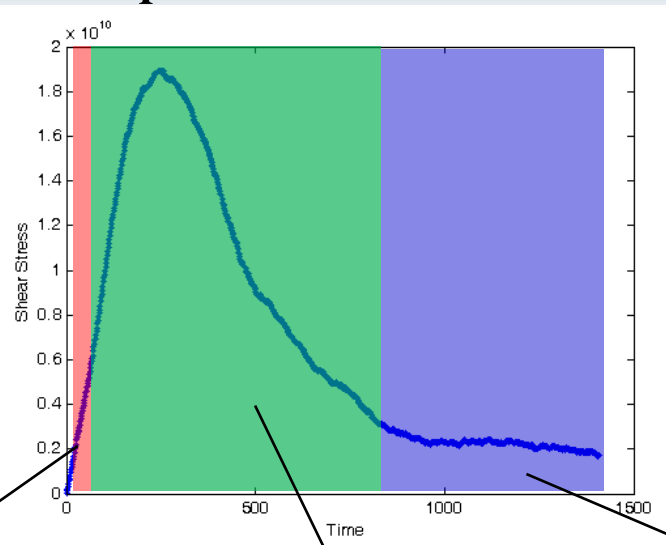


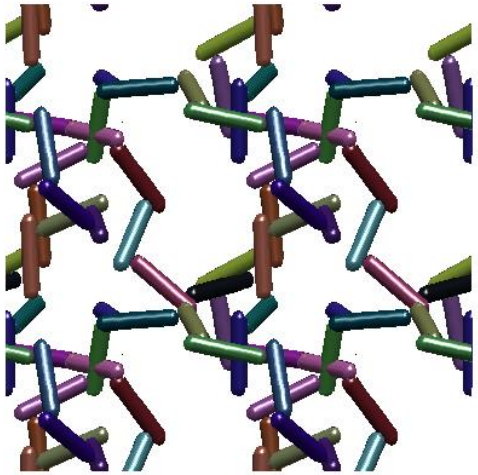
Gel-like Materials

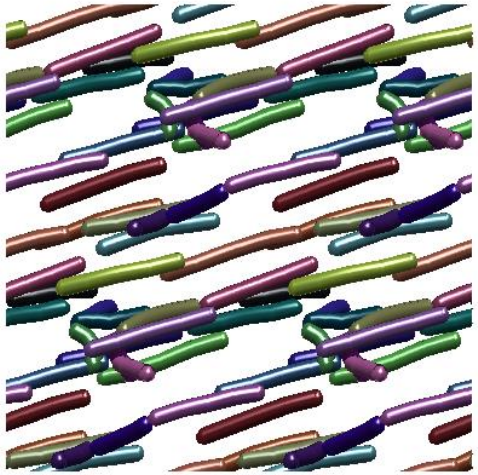


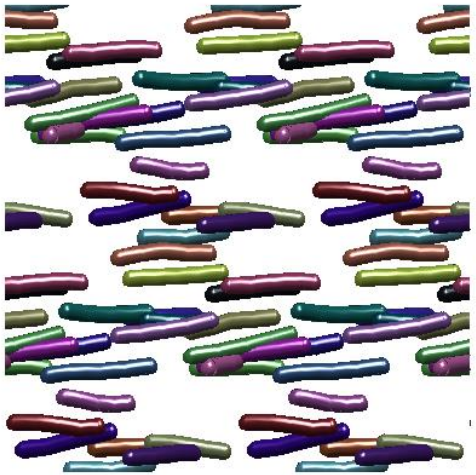
Gel-like Materials

Time Dependence of Shear Stress





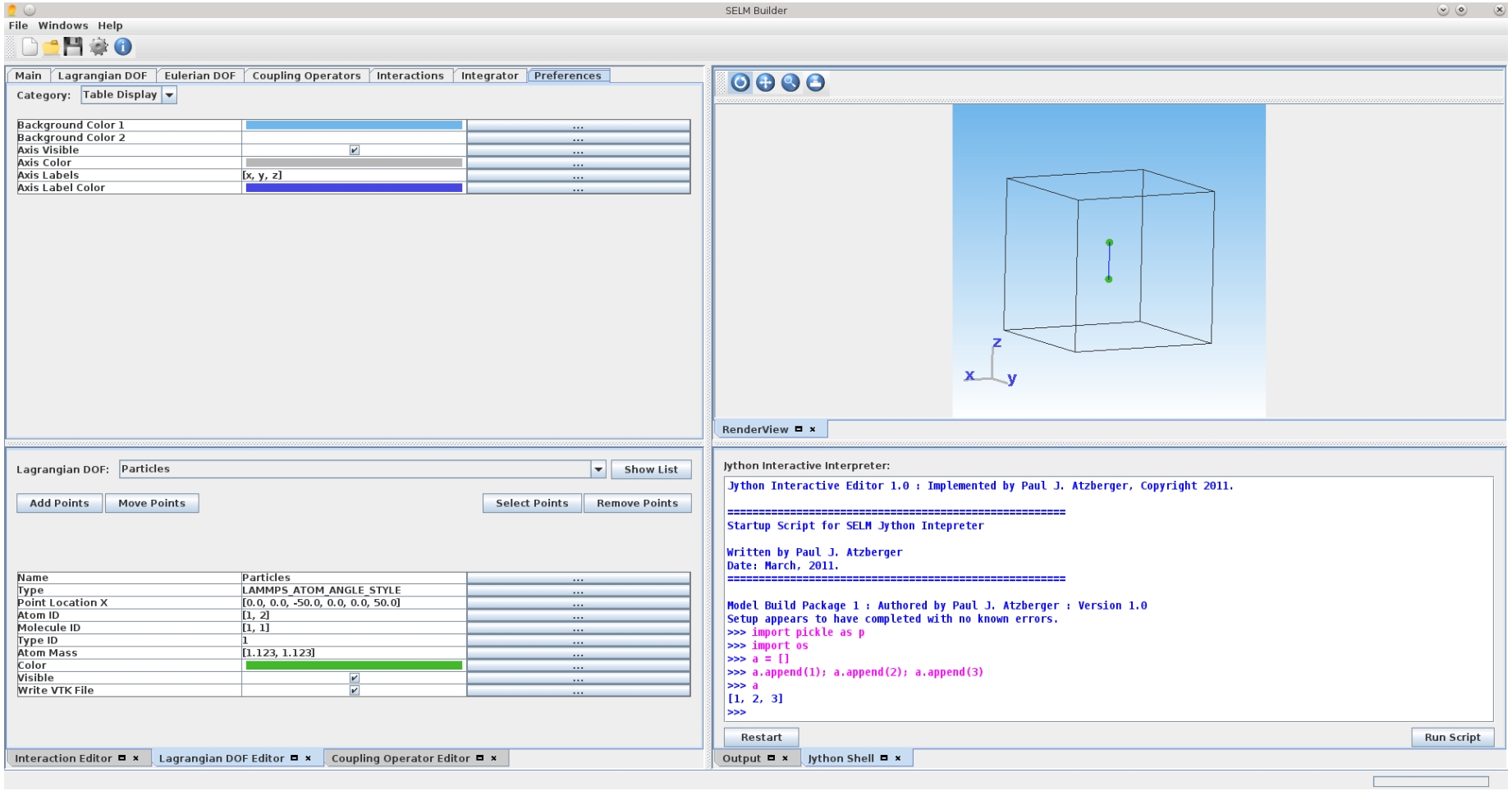




Mango-Selm GUI
(previous versions)

MANGO-SELM Simulation Software

MANGO - Modeling Software:



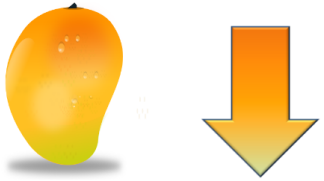
Atzberger 2016

MANGO-SELM Simulation Software

MANGO-SELM – Download: http://mango-selm.org/

Mango-Selm | Fluctuating Hydrodynamics

Home Downloads Screenshots Gallery Documentation Developers Forum About



Downloads

Please join our mailing list for the announcement of updated releases.

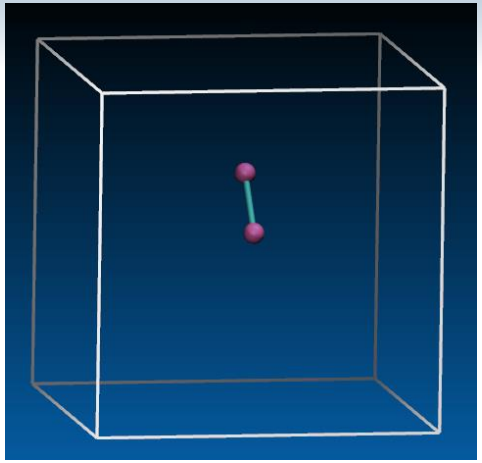
- Download Latest Release

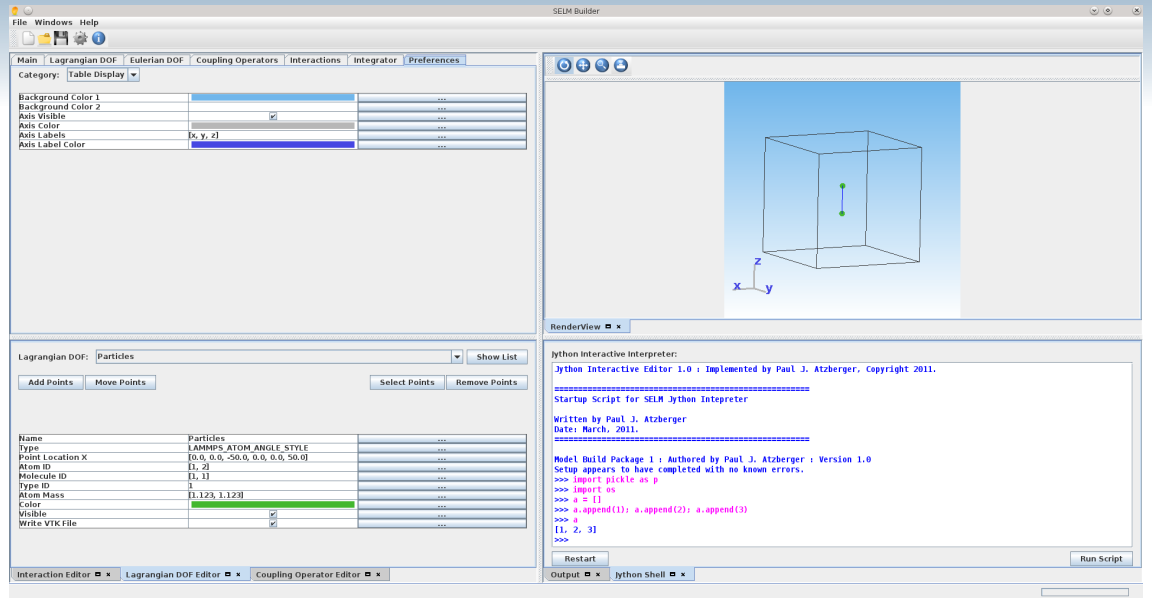
Additional Information

- Installation Instructions
- Tutorials for Setting up Simulations
- Mango-Selm Announcements
- Mango-Selm Discussion Forum
- Mango-Selm Issue Tracker

MANGO-SELM Simulation Software

Demo Live: FENE_Dimer





Steps:

1. Use File→Open project.
2. Load: FeneTest1/FeneModel.SELM_Builder_Project
3. Adjust coupling operator table to /common/CouplingOp_T_KERNEL_1.SELM_CouplingOperator_weightTable
4. Gear Icon → generate SELM simulation files.
5. Link executable in ln –s ../common/SELM_LAMMPS_2.0.0a_serial_x86_Ubuntu run
6. run –in Fene_Dimer.LAMMPS_script
7. Generates output data → .dcd file.
8. Run ./vis_FENE.vmd to visualize the model.

Important files:

FENE_Dimer.LAMMPS_script
FENE_Dimer.LAMMPS_read_data
FENE_Dimer.SELM_Info
FENE_Dimer.SELM_InfoExtra
FENE_Dimer.SELM_params
FENE-bonds.SELM_Interaction

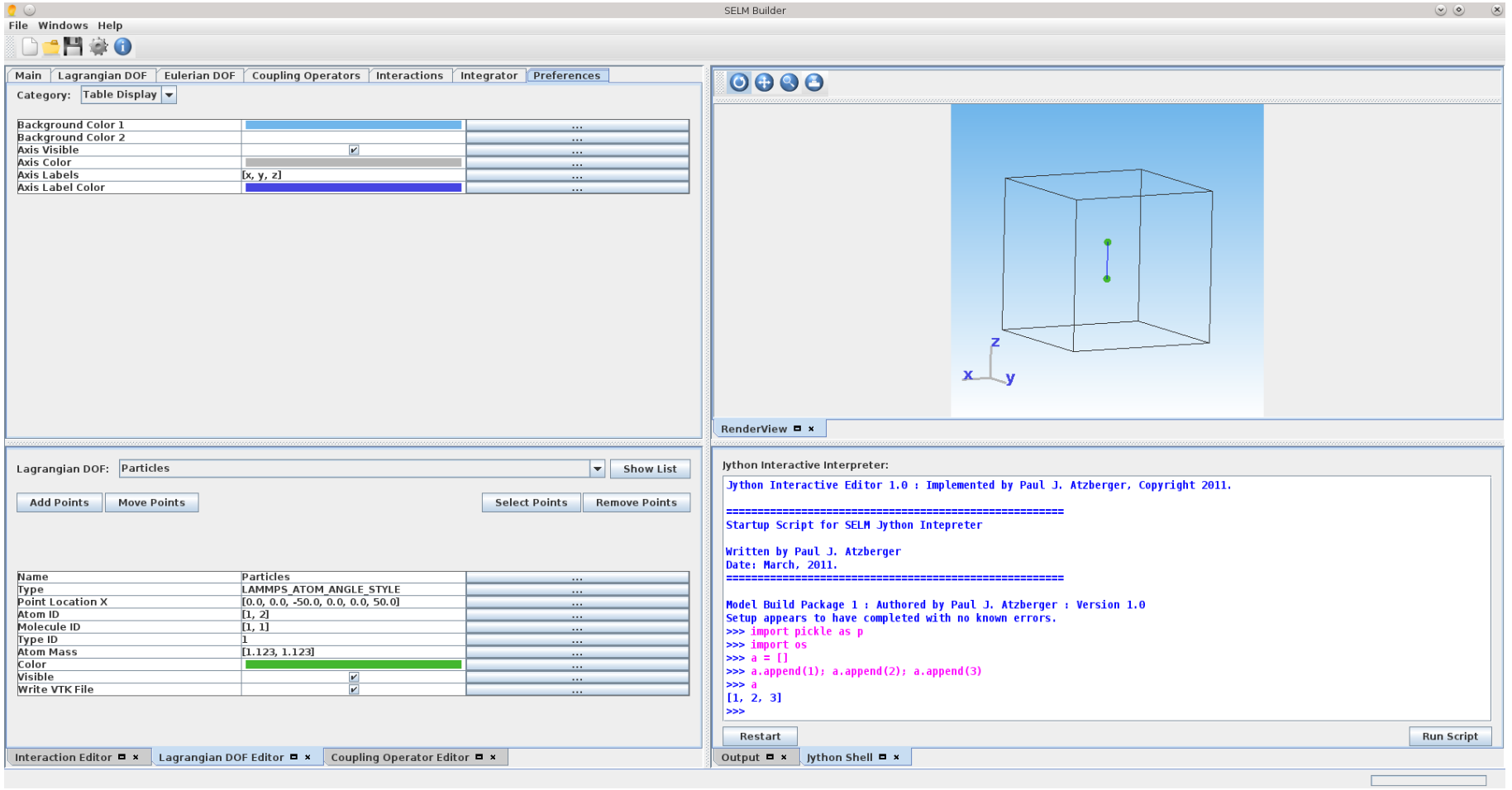
CouplingOp.SELM_CouplingOperator
CouplingOp_T_KERNEL_1.SELM_CouplingOperator_weightTable

LAMMPS_SHEAR_QUASI_STEADY1_FFTW3.SELM_Integrator
LAMMPS_SHEAR_UNIFORM1_FFTW3.SELM_Eulerian
Particles.SELM_Lagrangian

SELM_LAMMPS_serial_x86_Ubuntu
*.dcd
vis1.vmd

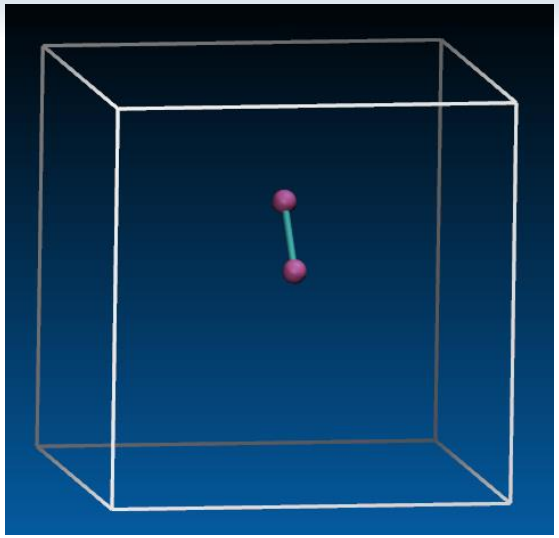
MANGO-SELM Simulation Software

Demo Live: FENE

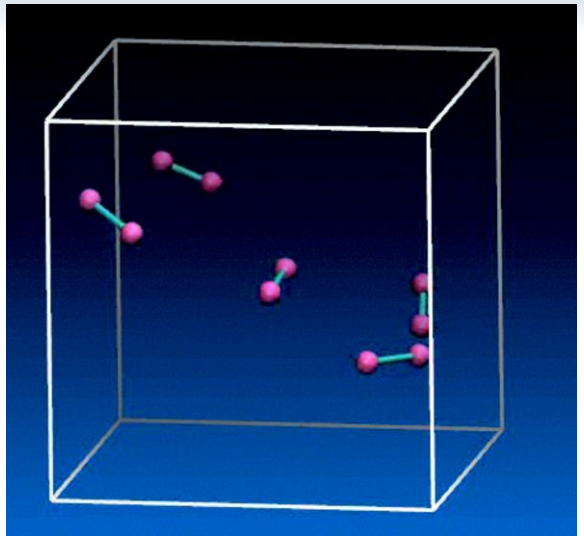


MANGO-SELM Simulation Software

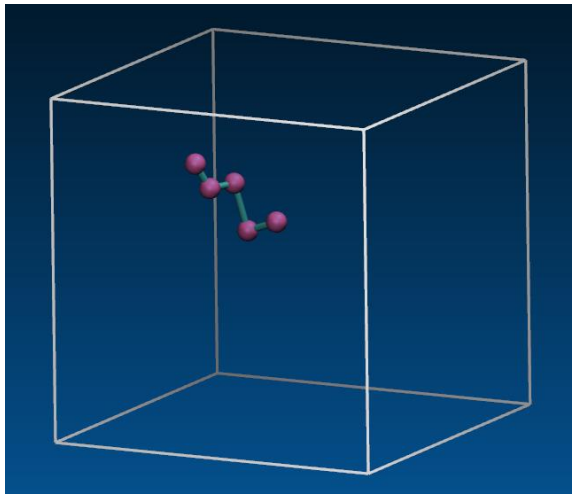
Other Demos:



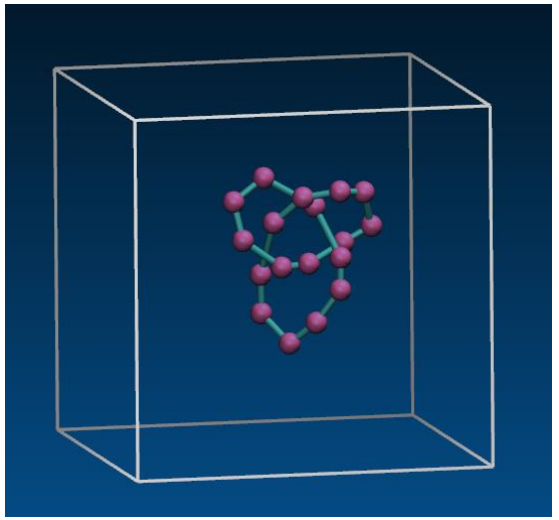
Sheared FENE Dimer



FENE Fluid



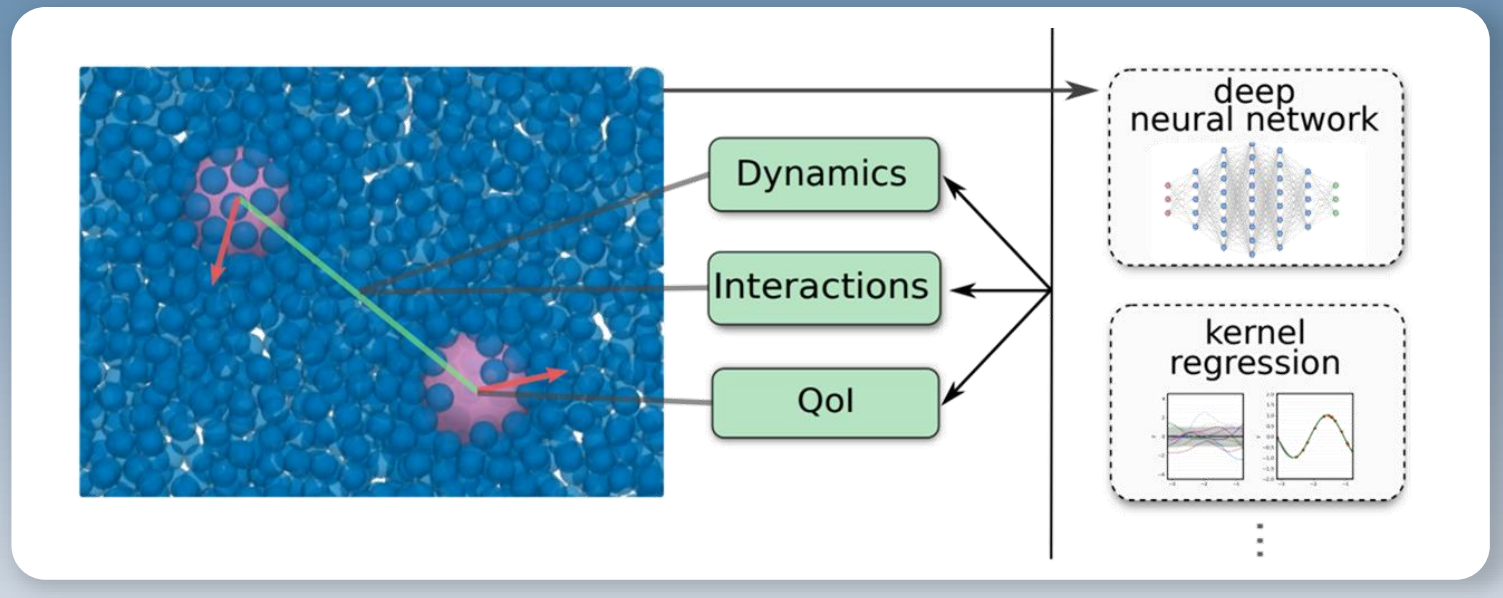
Polymer Chain

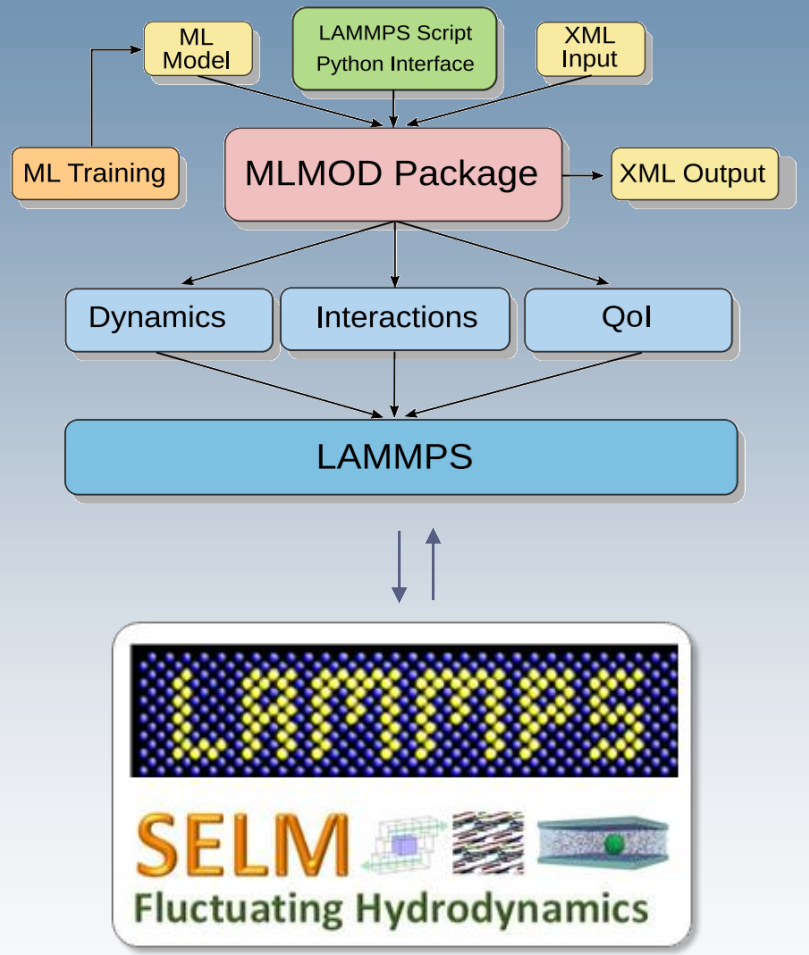


Polymer Knot

MLMOD Package

MLMOD Package: Machine Learning Methods for Data-Driven Modeling





LAMMPS Workshop
August 2021

Paul J. Atzberger
University of California Santa Barbara

DOE ASCR PhILMS
DE-SC0019246

NSF Grant
DMS - 1616353

http://software.atzberger.org
paper: https://arxiv.org/abs/2107.14362

MLMOD Package: Data-Driven Modeling

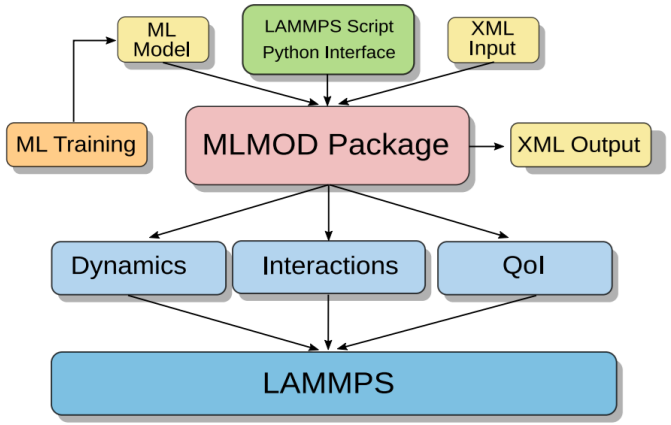
Software

MLMOD
Machine Learning Modeling Package

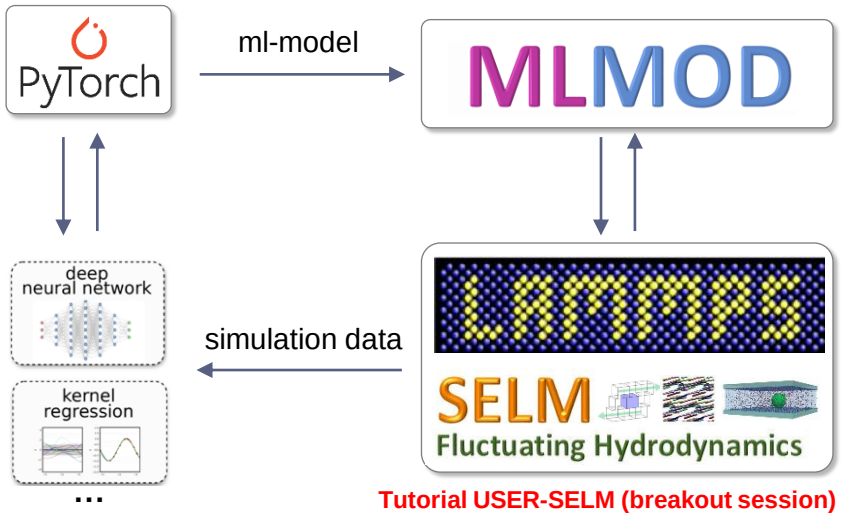
C/C++ python PyTorch jupyter notebooks

http://software.atzberger.org
paper: https://arxiv.org/abs/2107.14362

Package Structure



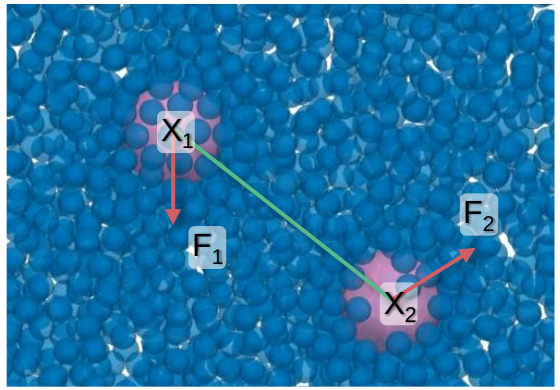
Machine Learning (training) / Scientific Computation (simulation)



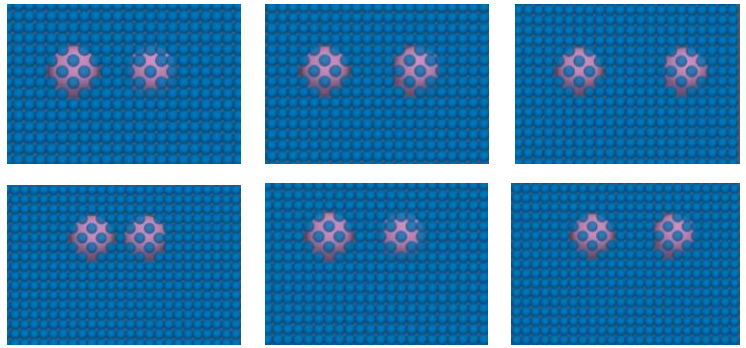
Tutorial USER-SELM (breakout session)
Friday, 8/13, 12:50pm EDT

Example use case

Colloid + Solvent System



Simulation Data



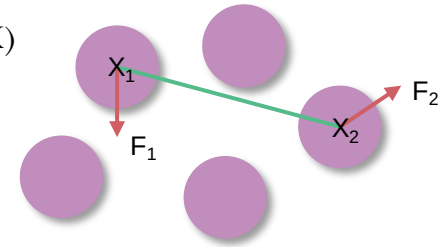
...

Reduced Model

$$\frac{d\mathbf{X}}{dt} = \mathbf{M}F + k_B T \nabla_X \cdot \mathbf{M} + \mathbf{F}_{thm}$$

$$\langle \mathbf{F}_{thm}(s)\mathbf{F}_{thm}(t)^T \rangle = 2k_B T \mathbf{M}\delta(t-s).$$

M=M(X)



paper: https://arxiv.org/abs/2107.14362

More Information:
http://software.atzberger.org

DOE ASCR PhILMS DE-SC0019246

NSF Grant DMS - 1616353

Summary / Conclusions

Conclusions

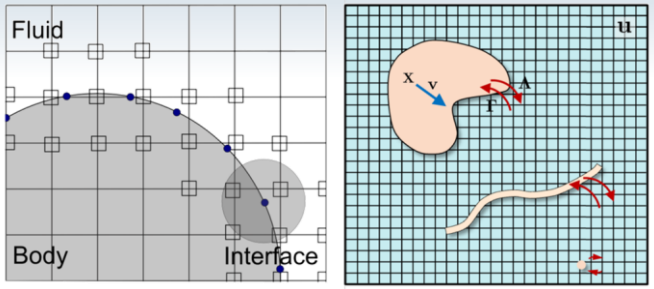

B. Gross

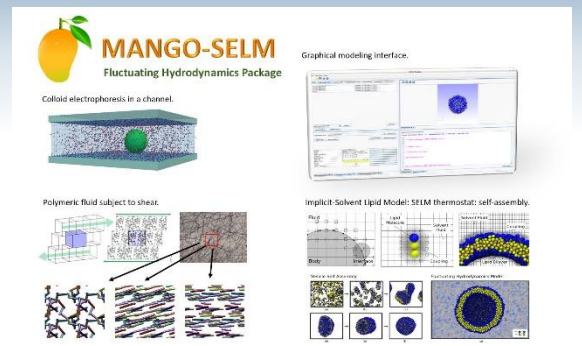

D. Rower

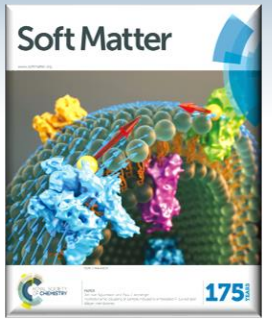

M. Padidar


J. Sigurdsson

UCSB Recent Student Collaborators







Paper
2016 Atzberger & Sigurdsson

Summary

Stochastic Immersed Boundary Methods *with numerical solvers preserving statistical mechanics properties.*

Stochastic Eulerian Lagrangian Methods *for inertial and overdamped regimes, various boundary conditions.*

Python interface *for setting up simulations,* ***LAMMPS molecular dynamics integration*** *(modeling, analysis).*

Applications *in soft materials, complex fluids, rheology, microfluidics, biophysics, lipid bilayer membranes.*

Mango-Selm package for Fluctuating Hydrodynamics
http://atzberger.org

Sandia LAMMPS Molecular Dynamics

Papers

A Stochastic Immersed Boundary Method for Fluid-Structure Dynamics at Microscopic Length Scales,
P.J. Atzberger, P.R. Kramer, and C.S. Peskin, J. Comp. Phys., Vol. 224, Iss. 2, (2007).

Stochastic Eulerian Lagrangian Methods for Fluid Structure Interactions with Thermal Fluctuations,
P.J. Atzberger, J. of Comp. Phys., 230, pp. 2821--2837, (2011).

Surface Fluctuating Hydrodynamics Methods for the Drift-Diffusion Dynamics of Particles and Microstructures within Curved Fluid Interfaces,
D. Rower, M. Padidar, and P. J. Atzberger, arXiv:1906.01146, (2019).

Meshfree Methods on Manifolds for Hydrodynamic Flows on Curved Surfaces: A Generalized Moving Least-Squares (GMLS) Approach,
Gross B. J., Kuberry P. A., Trask N., Atzberger P. J., J. Comp. Phys., 409, 15 May (2020).

UCSB Recent Student Collaborators

B. Gross, M. Padidar, D. Rower, J. K. Sigurdsson.

Sandia Collaborators

N. Trask, P. Kuberry, J. Hu, C. Siefert, and others.

Funding

DOE ASCR CM4
DE-SC0009254

DOE ASCR PhILMS
DE-SC0019246

NSF Grant
DMS - 1616353

NSF CAREER Grant
DMS-0956210

More information: http://atzberger.org/

Publications

A Stochastic Immersed Boundary Method for Fluid-Structure Dynamics at Microscopic Length Scales,
P.J. Atzberger, P.R. Kramer, and C.S. Peskin, J. Comp. Phys., Vol. 224, Iss. 2, (2007). http://dx.doi.org/10.1016/j.jcp.2006.11.015

Stochastic Eulerian Lagrangian Methods for Fluid Structure Interactions with Thermal Fluctuations,
P.J. Atzberger, J. of Comp. Phys., 230, pp. 2821--2837, (2011). http://dx.doi.org/10.1016/j.jcp.2010.12.028

Fluctuating Hydrodynamics Methods for Dynamic Coarse-Grained Implicit-Solvent Simulations in LAMMPS, Y. Wang, J. K. Sigurdsson, and P.J. Atzberger, SIAM J. Sci. Comp. (accepted), (2016). https://doi.org/10.1137/15M1026390

MLMOD Package: Machine Learning Methods for Data-Driven Modeling in LAMMPS, P.J. Atzberger, arXiv (2021), https://arxiv.org/abs/2107.14362.

Surface Fluctuating Hydrodynamics Methods for the Drift-Diffusion Dynamics of Particles and Microstructures within Curved Fluid Interfaces,
D. Rower, M. Padidar, and P. J. Atzberger, arXiv:1906.01146, (2019). https://arxiv.org/abs/1906.01146

Meshfree Methods on Manifolds for Hydrodynamic Flows on Curved Surfaces: A Generalized Moving Least-Squares (GMLS) Approach,
Gross B. J., Kuberry P. A., Trask N., Atzberger P. J., J. Comp. Phys., 409, 15 May (2020). https://doi.org/10.1016/j.jcp.2020.109340

Systematic Stochastic Reduction of Inertial Fluid-Structure Interactions subject to Thermal Fluctuations, G. Tabak and P.J. Atzberger, SIAM J. Appl. Math., 75(4), 1884–1914, (2015). http://dx.doi.org/10.1137/15M1019088

Dynamic Implicit-Solvent Coarse-Grained Models of Lipid Bilayer Membranes : Fluctuating Hydrodynamics Thermostat, Y. Wang, J. K. Sigurdsson, E. Brandt, and P.J. Atzberger, Phys. Rev. E 88, 023301, (2013). http://dx.doi.org/10.1103/PhysRevE.88.023301

Spatially Adaptive Stochastic Methods for Fluid-Structure Interactions Subject to Thermal Fluctuations in Domains with Complex Geometries,
P. Plunkett, J. Hu, C. Siefert, P.J. Atzberger, Journal of Computational Physics, Vol. 277, 15 Nov. 2014, pg. 121--137, (2014).
http://dx.doi.org/10.1016/j.jcp.2014.07.051

Incorporating Shear into Stochastic Eulerian Lagrangian Methods for Rheological Studies of Complex Fluids and Soft Materials,
P.J. Atzberger, Physica D, Vol. 265, pg. 57–70, (2013). http://dx.doi.org/10.1016/j.physd.2013.09.002

For additional information: http://atzberger.org/